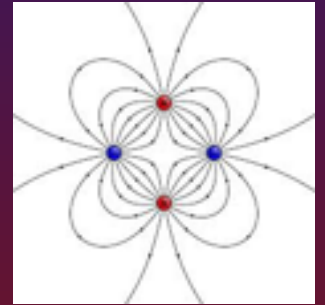
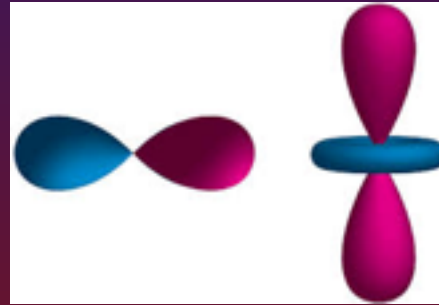
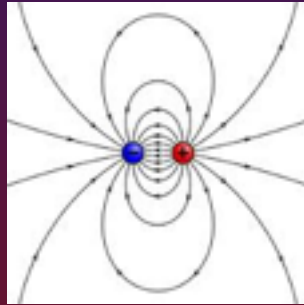
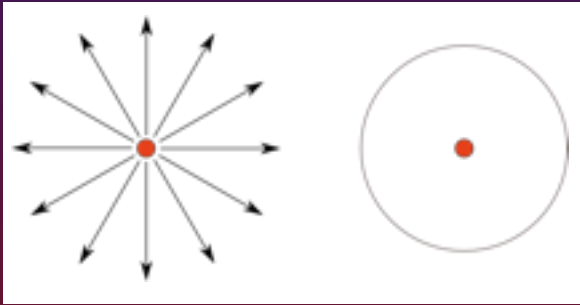


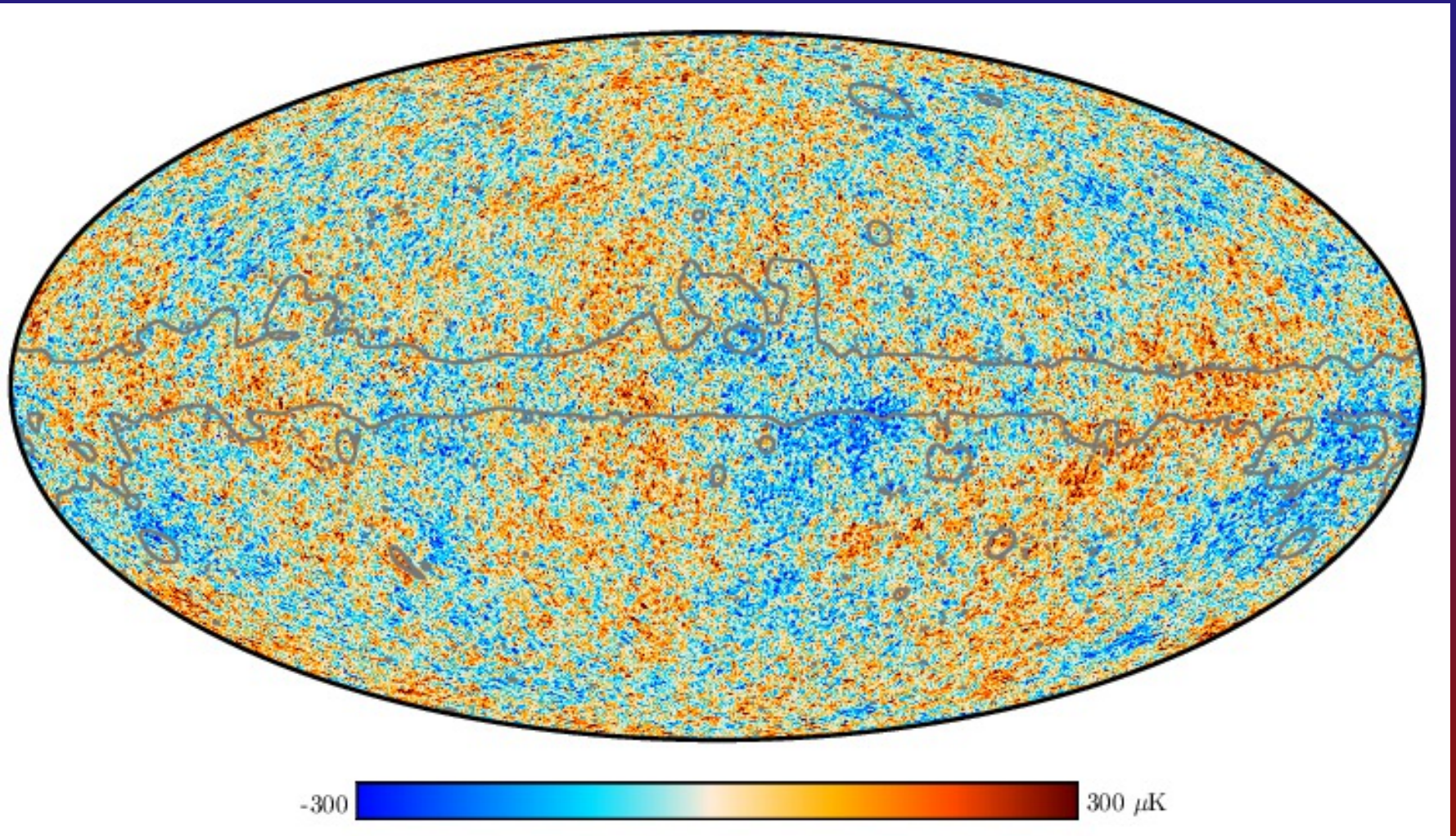
# The CMB's lowest-order multipoles



Douglas Scott  
UBC

# The CMB Sky

Temperature anisotropies at  $\sim 400,000$  years



# Statistical description of anisotropies

Expand sky in spherical harmonics

$$T(\theta, \phi) = \sum_{\ell m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

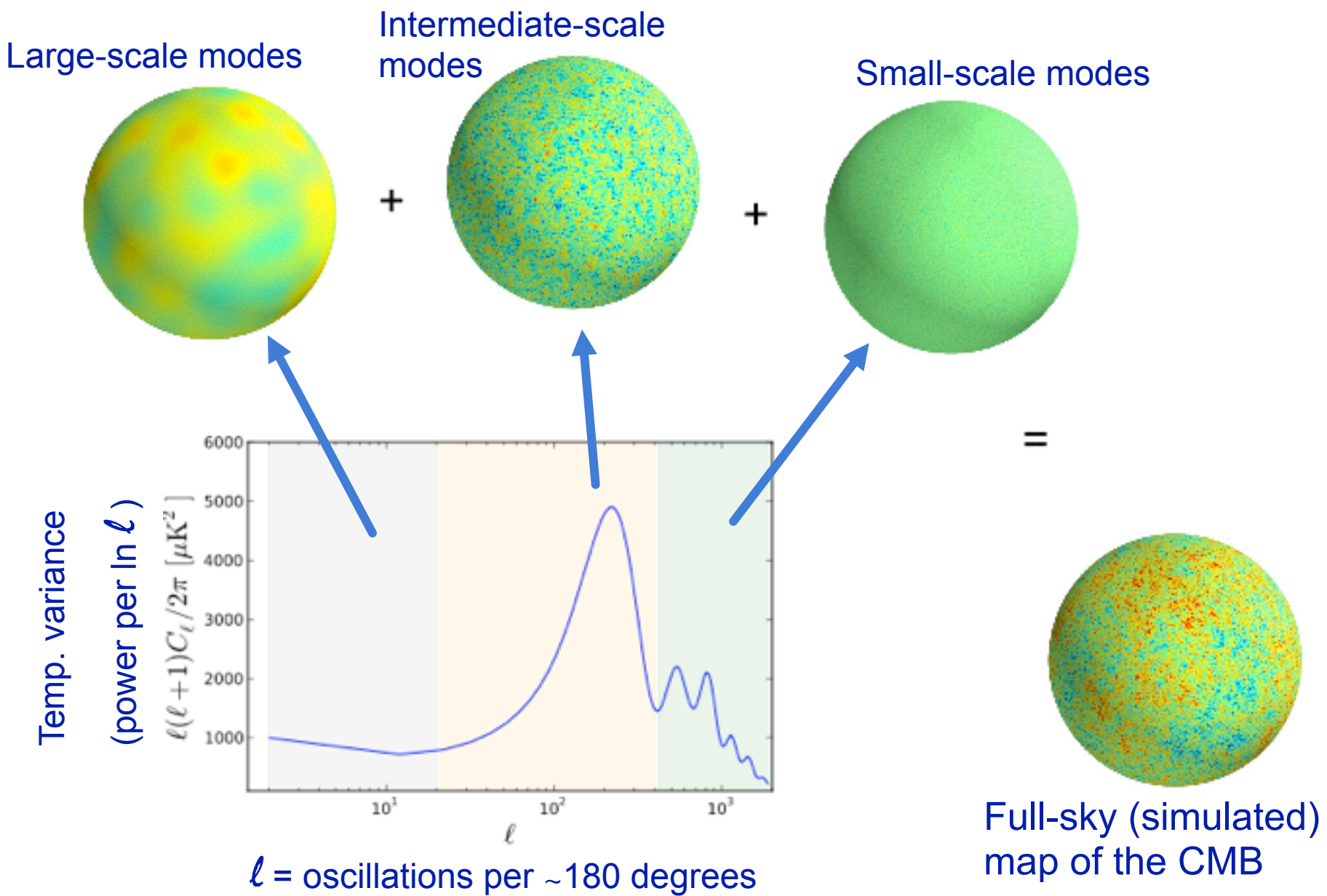
Monopole is  $T_0$  ( $=a_{00}$ )

Dipole is our “absolute motion”

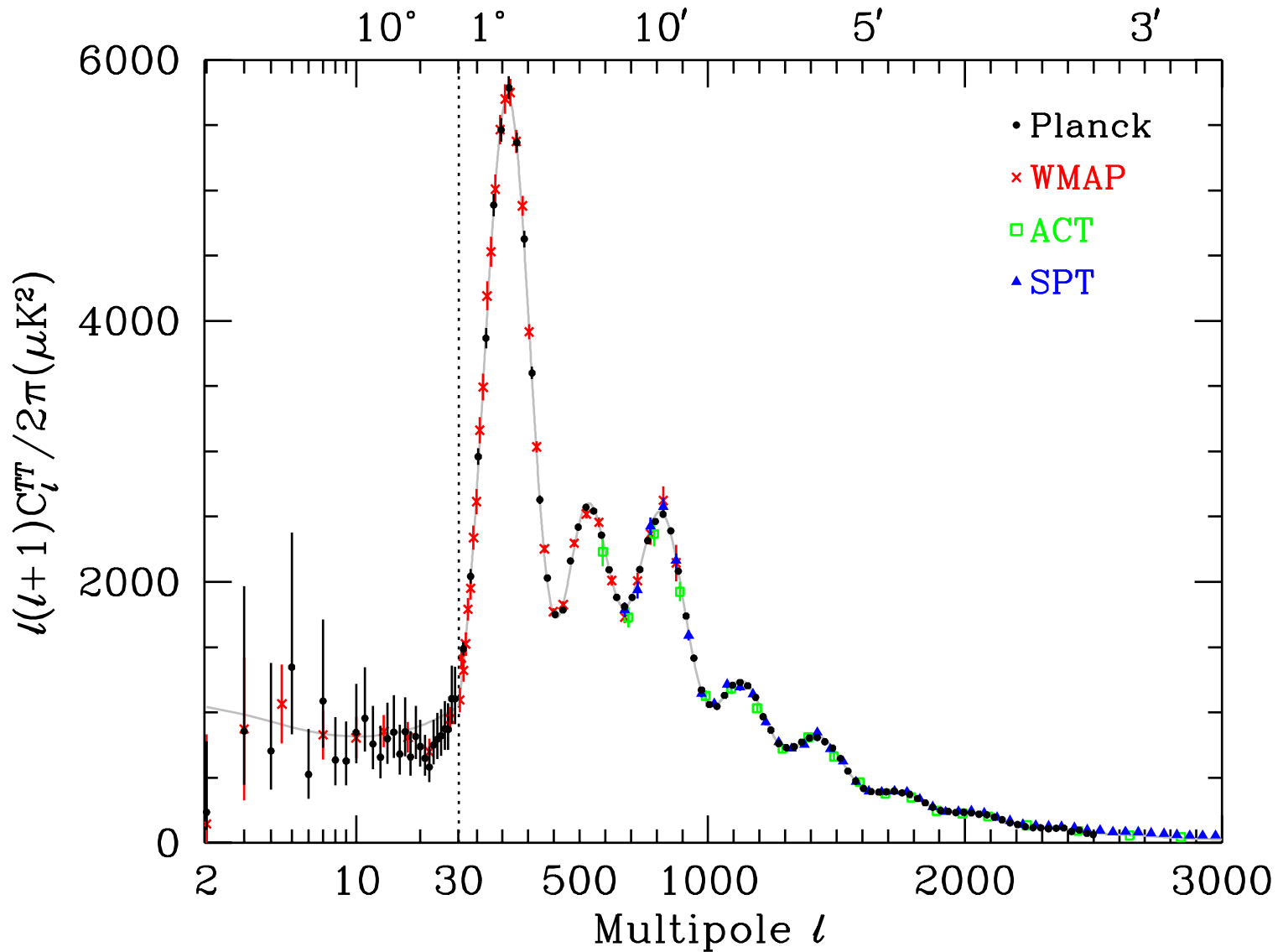
$\ell \geq 2$  modes give info on perturbations

$$C_\ell \equiv \langle |a_{\ell m}|^2 \rangle \quad \text{i.e. average over } m\text{s}$$

$$(2\ell + 1)C_\ell / 4\pi \quad \text{is power at each } \ell$$



# “Precision era” of cosmology



Angular scale

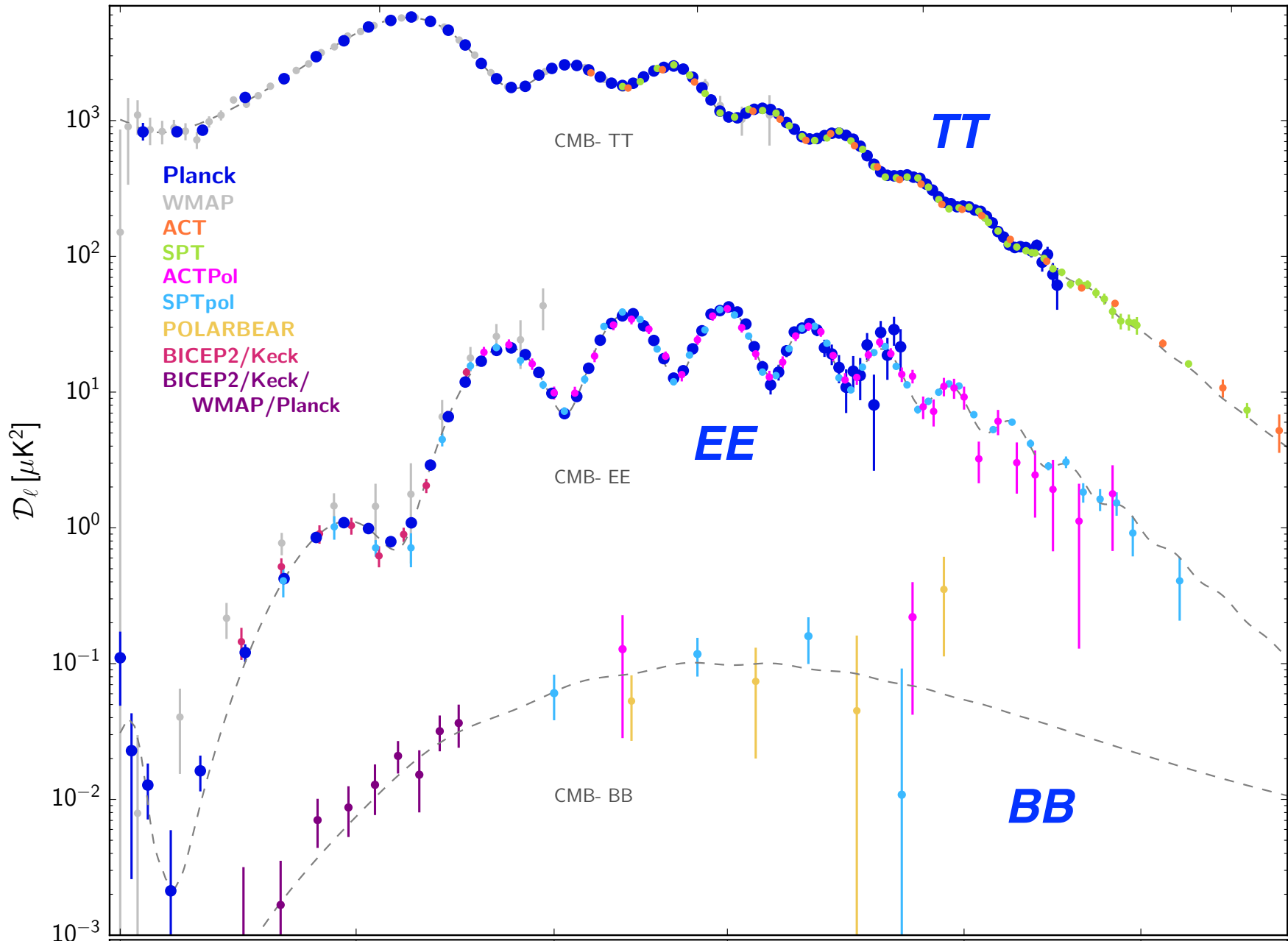
90°

1°

0.2°

0.1°

0.05°

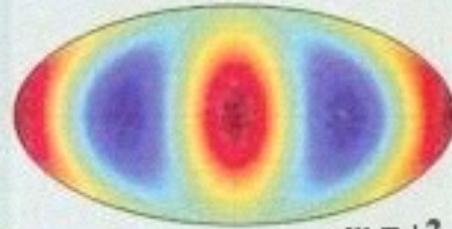


But let's ignore all that  
beauty and precision!

And talk about the  
very lowest multipoles!

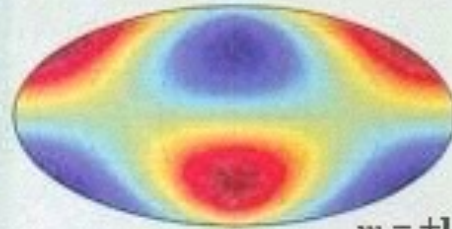


Monopole,  $l = 0, m = 0$  ↑



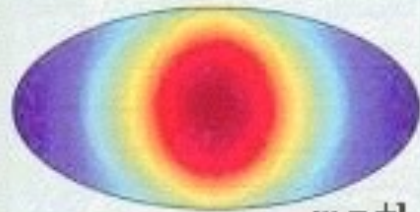
$m = +2$

Quadrupole,  $l = 2$  →

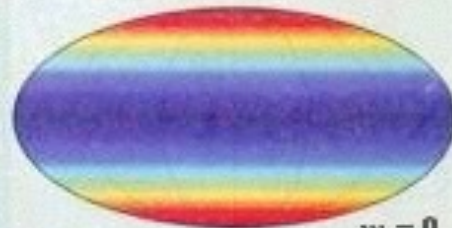


$m = +1$

Dipole,  $l = 1$  ↓



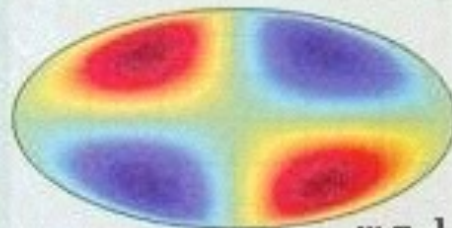
$m = +1$



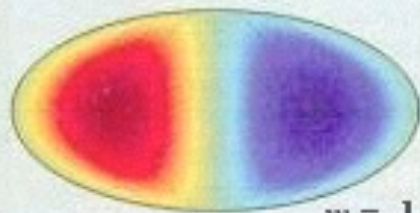
$m = 0$



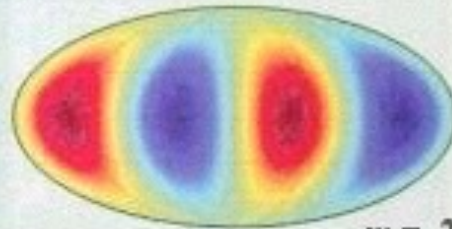
$m = 0$



$m = -1$



$m = -1$



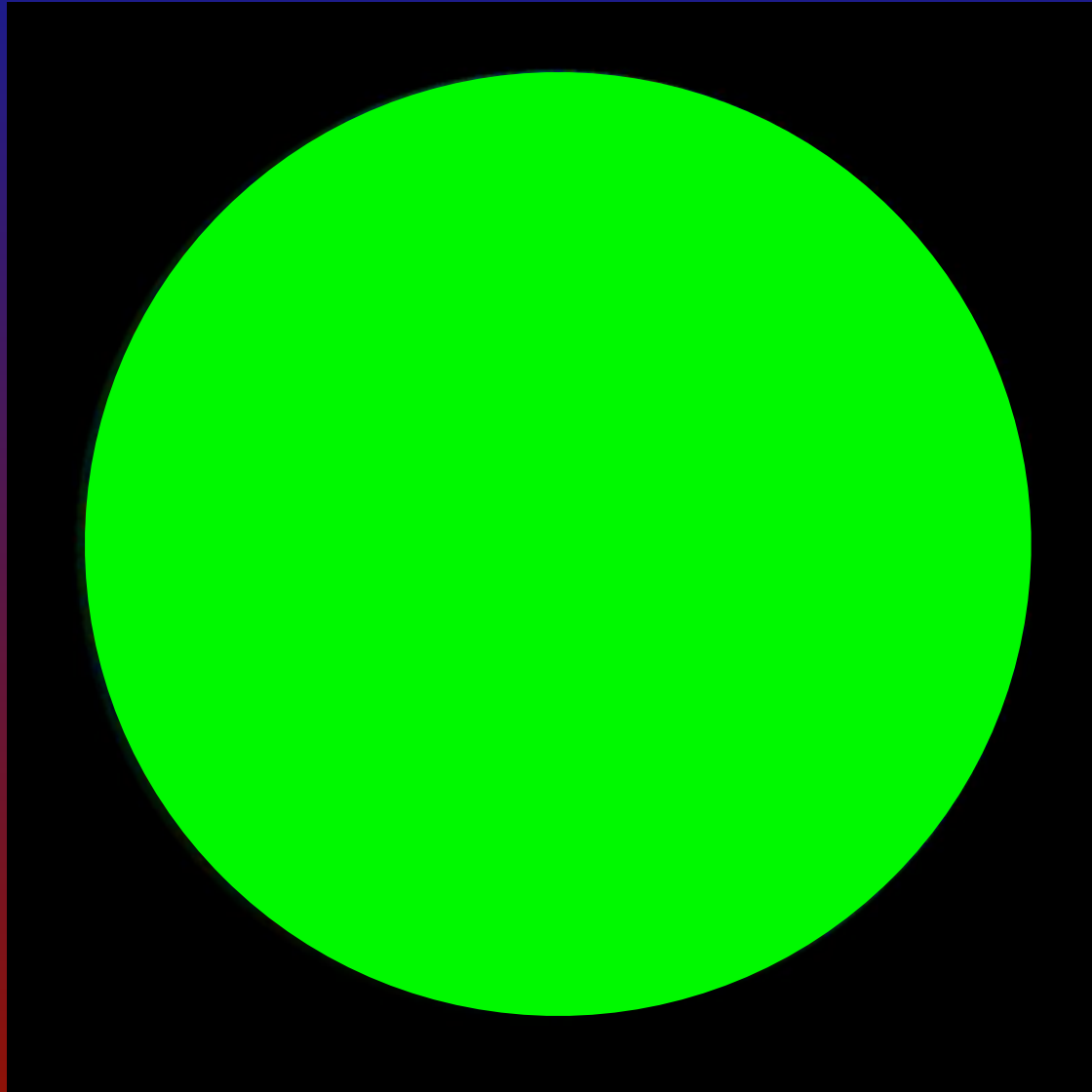
$m = -2$

Lowest-order spherical harmonics

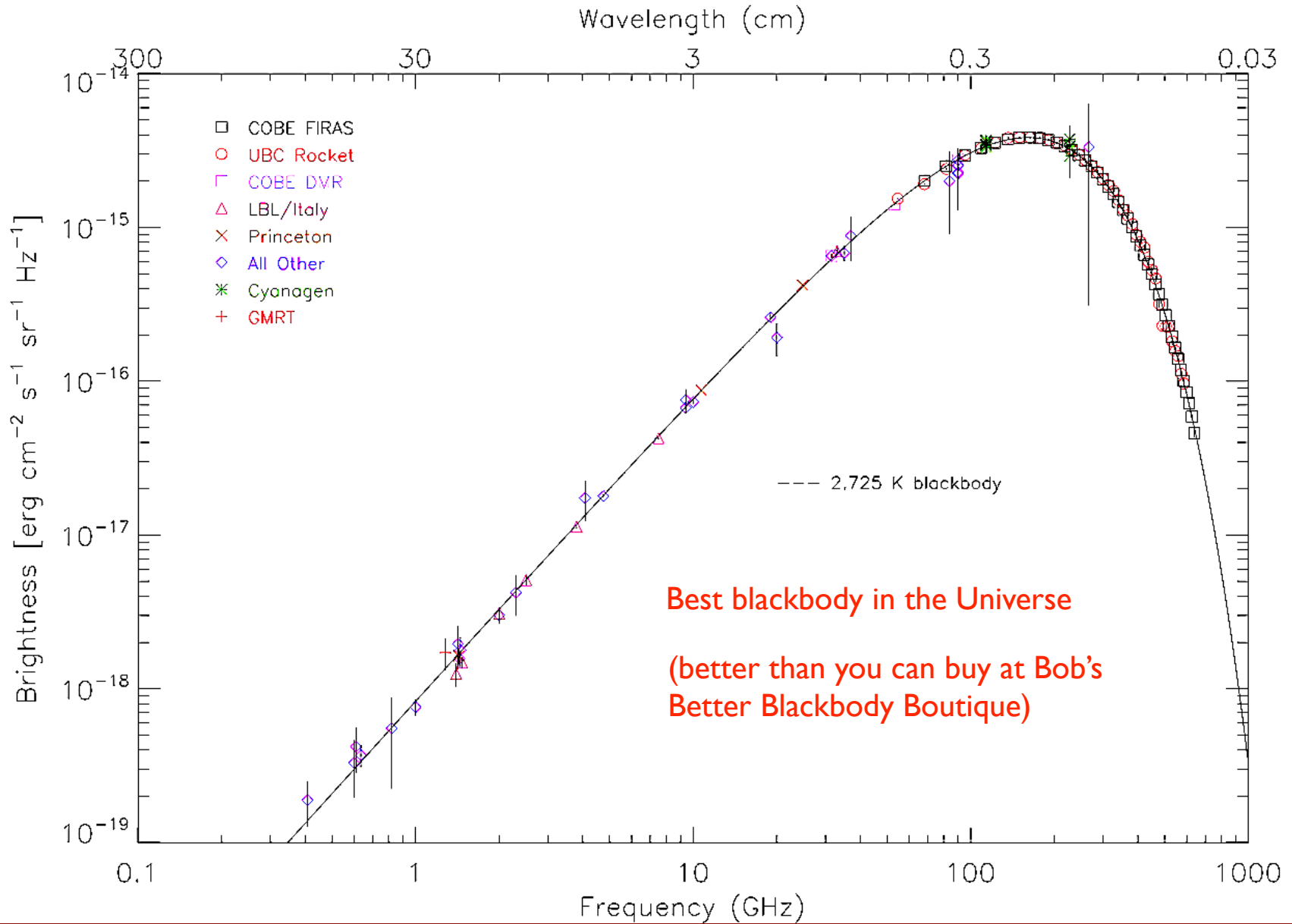
Let's start with the monopole

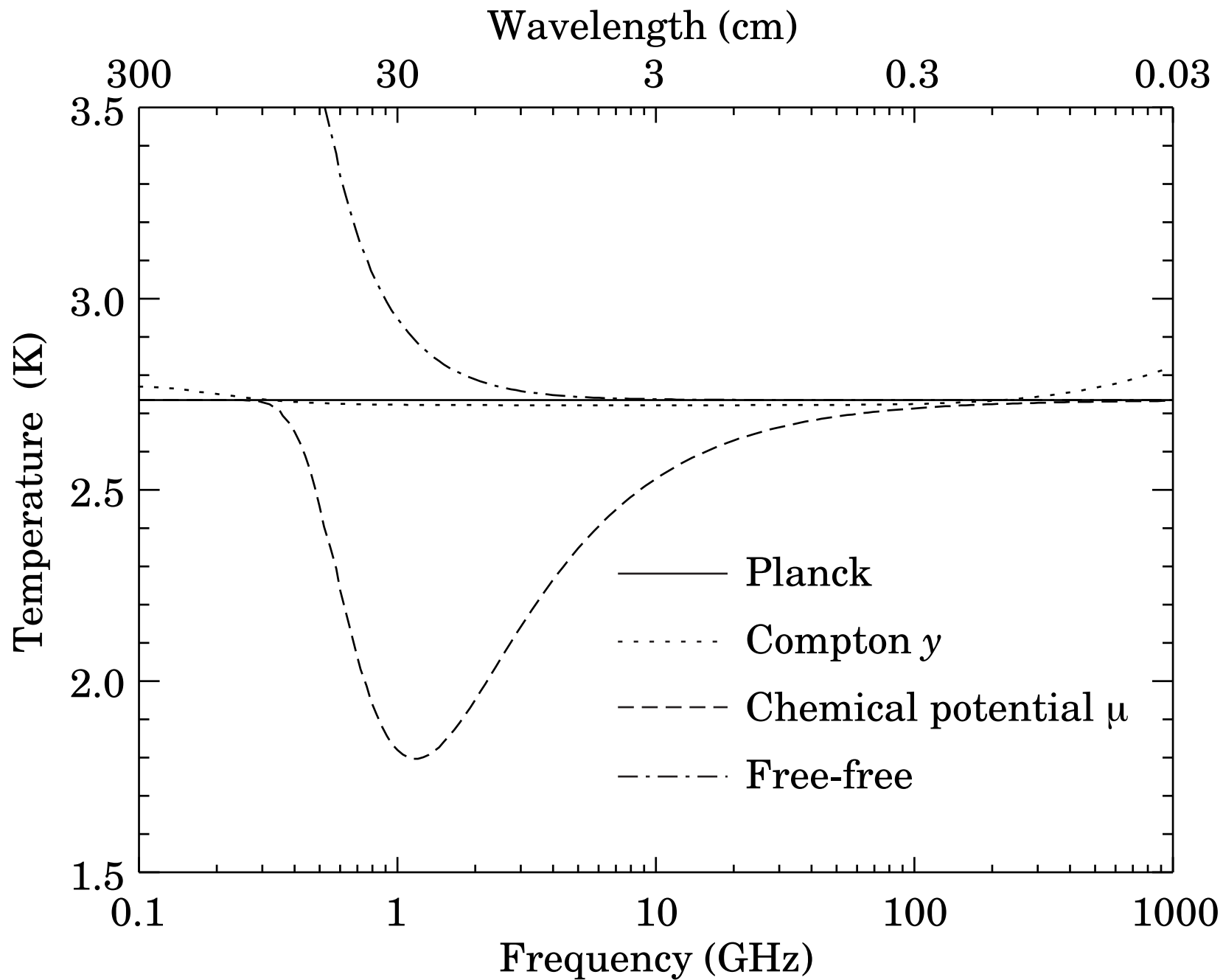


# CMB Sky



# CMB Spectrum





# CMB Spectrum

$$T_0 = 2.7255 \pm 0.0006 \text{ K}$$

$$n_0 = 410.1 \text{ cm}^{-3}$$

$$\epsilon_0 = 0.2605 \text{ eV cm}^{-3}$$

$$\nu_{\text{peak}} = 160.24 \text{ GHz}$$

$$|y| < 1.2 \times 10^{-5} \quad (95\% \text{ CL})$$

$$T_0 = -270.4245 \text{ C}$$

$$|\mu_0| < 9 \times 10^{-5} \quad (95\% \text{ CL})$$

$$T_0 = -454.7641 \text{ F}$$

$$|Y_{ff}| < 1.9 \times 10^{-5} \quad (95\% \text{ CL})$$

(20). For example, the CMB temperature can be expressed dimensionlessly as a fraction of the electron mass,  $\Theta = kT_0/m_e c^2 \simeq 4.6 \times 10^{-10} \simeq 2^{-31} \simeq \alpha^4/(2\pi)$ , or  $2.5 \times 10^{-13} \sim e^{-29}$  in terms of the proton mass.

Tight constraints on distortions  
But expected distortions smaller still

# Where did the CMB temperature come from?

$T_0 = 2.7255 \pm 0.0006$  K  
(Fixsen 2009)

$$e \text{ Kelvin} (= 2.718 \text{ K})$$

$$\sqrt{15/2} \text{ Kelvin} (= 2.739 \text{ K})$$

$$30/11 \text{ Kelvin} (= 2.727 \text{ K})$$

$$-\ln(9\alpha) \text{ Kelvin} (= 2.723 \text{ K})$$

$$\text{Triple point of water} \div 100 (= 2.7315 \text{ K})$$

$$(2\alpha/\pi)^4 m_e c^2 / k (= 2.762 \text{ K})$$

$$(2/5)(\alpha_G m_e / 2\pi m_p)^{1/4} m_p c^2 / k (= 2.719 \text{ K})$$

$$[\alpha_G \equiv Gm_e^2 / c\hbar] \quad 16\sqrt{2}\pi\alpha_G^{1/4} m_e c^2 / k (= 2.727 \text{ K})$$

$$(hc/k) \mu\text{Leagues}^{-1} (= 2.98 \text{ K})$$

$$[\pi e^\pi \simeq 73] \quad e^{-73} T_{PI} (= 2.805 \text{ K})$$

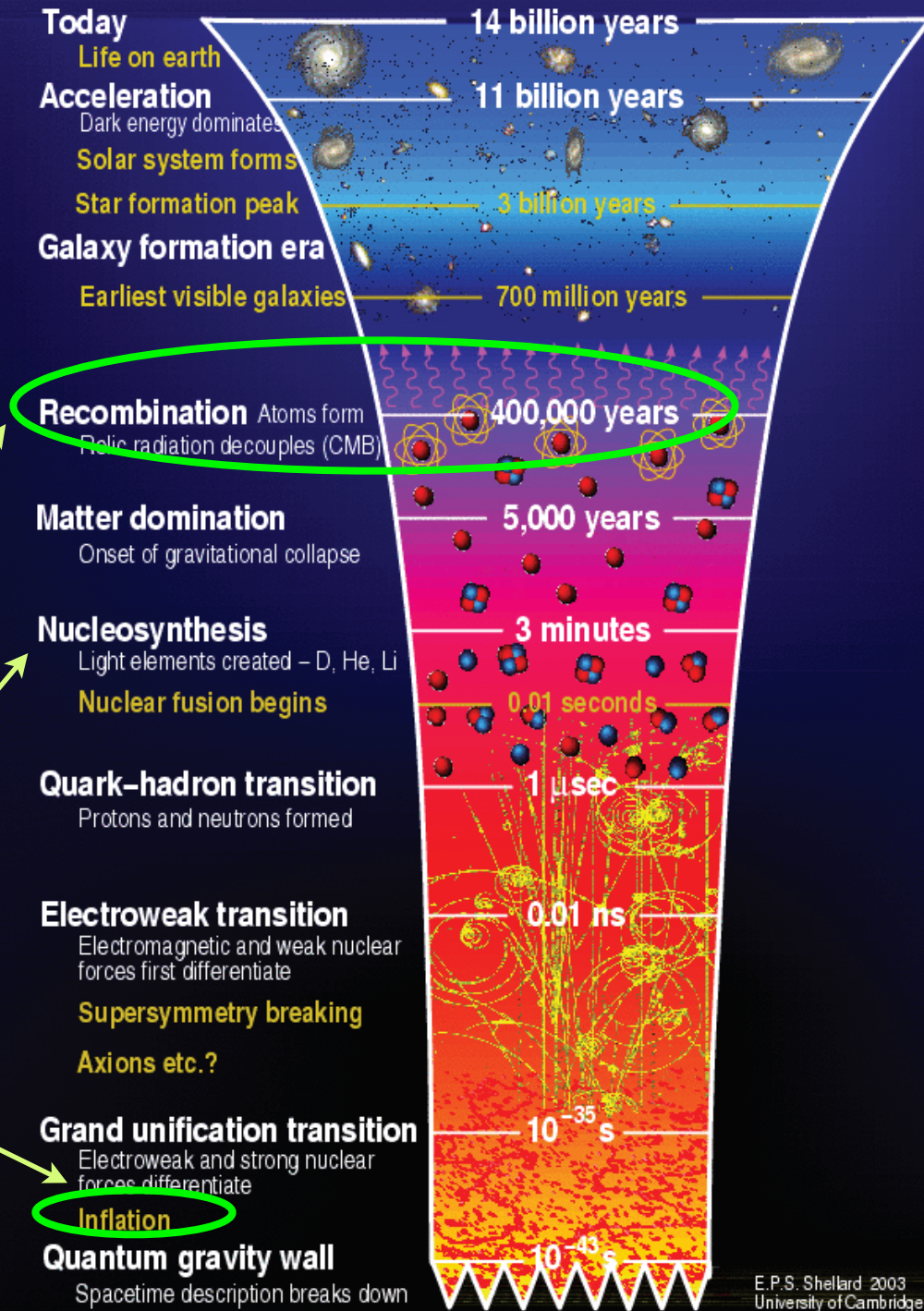
# The Hot Big Bang

Where did the CMB really come from?

Last scattered at this epoch

Photons made at this epoch

Deriving from physics at this epoch

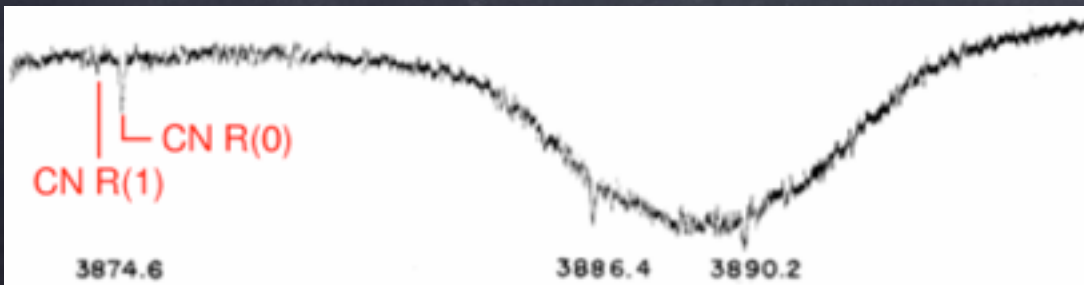


# CMB history (eh)



Andrew McKellar

CN measurements  
at DAO (1940, 1941)  
⇒ rotational  
temp  $\approx 2.3\text{K}$



Herzberg (1950):  
“...only a very  
restricted meaning”

# MEASUREMENTS OF ABSOLUTE SKY BRIGHTNESS TEMPERATURES AT 320 AND 707 MHz

By J. V. WALL,\*† T. Y. CHU,\*‡ and J. L. YEN\*

[*Manuscript received September 9, 1969*]

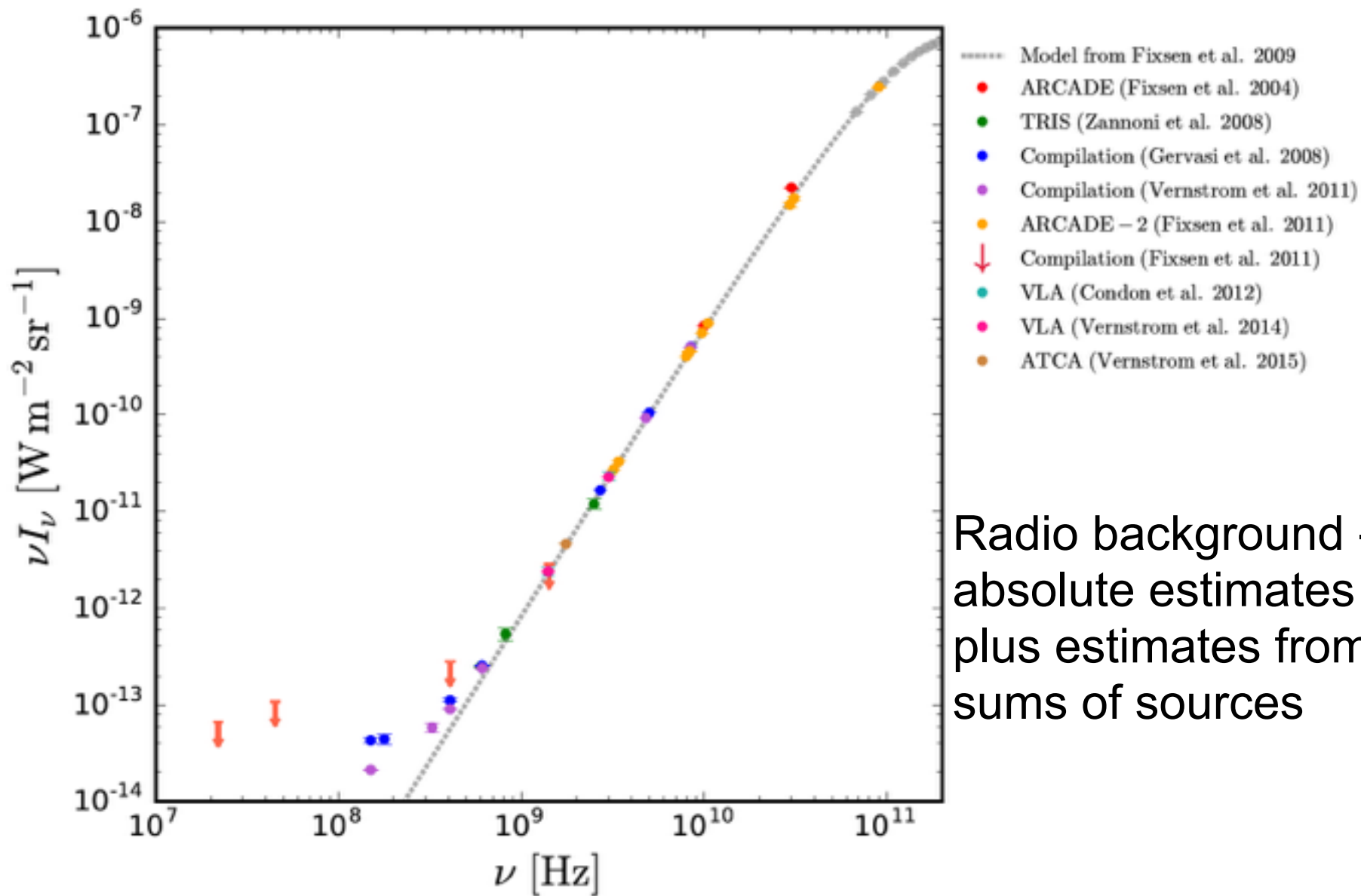
## *Abstract*

Measurements of absolute sky brightness temperatures have been carried out over limited regions of the sky at 320 and 707 MHz. At both frequencies low resolution horn antennas were used with Dicke switched receivers. Zero levels were determined with a substitution load at the temperature of liquid nitrogen. The antenna temperatures were reduced to full beam brightness temperatures by removing ground, side lobe, and atmospheric contributions.

The results indicate a change in spectrum in this frequency range consistent with addition to the galactic nonthermal radiation of isotropic radiation having a thermal spectrum and a brightness temperature of 3°K. A power law spectral index of  $-0.45 \pm 0.15$  is obtained for the galactic nonthermal emission.

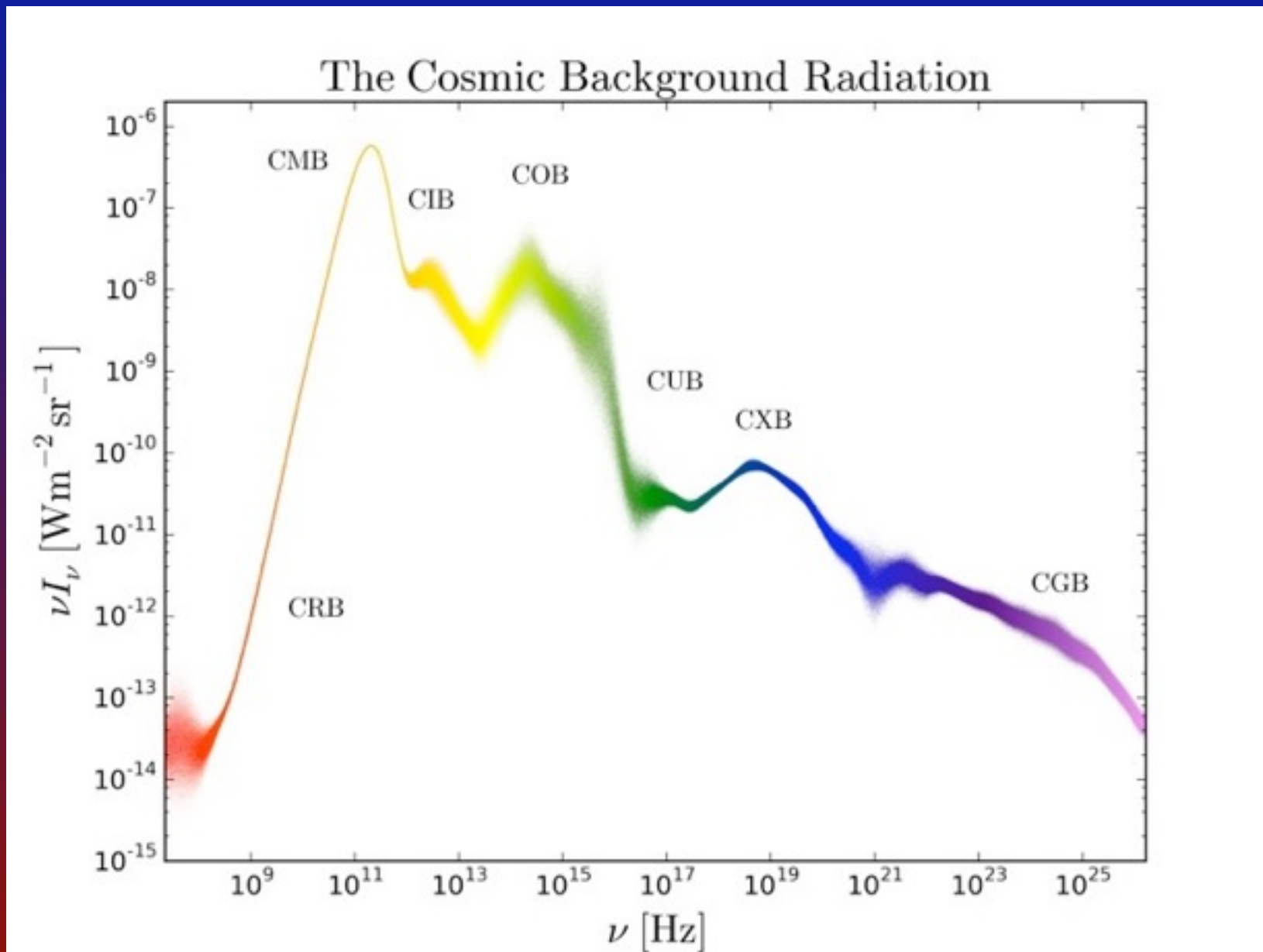
Jasper's contribution (data taken in 1965)





Radio background -  
 absolute estimates  
 plus estimates from  
 sums of sources

# The (extragalactic) monopole across the entire EM spectrum



# The CMB monopole

Current measurement:  $T_0=2.7255\pm 0.0006\text{K}$   
(Fixsen 2009)

But  $\Delta T/T \sim 0.00001$  on all scales  
including our Hubble patch!

So if we could live in a  $\sim 3\sigma$  fluctuation  
then we're only  $\sim 10$  from Cosmic Variance!

But isn't the monopole coordinate dependent?

# The CMB monopole

But we live in a potential (which is in another potential ...)

So the “true” CMB monopole isn't what we measure anyway

(But this is only of order  $v^2/c^2$ )

And this helps underscore that it's coordinate-dependent

# Defining the monopole

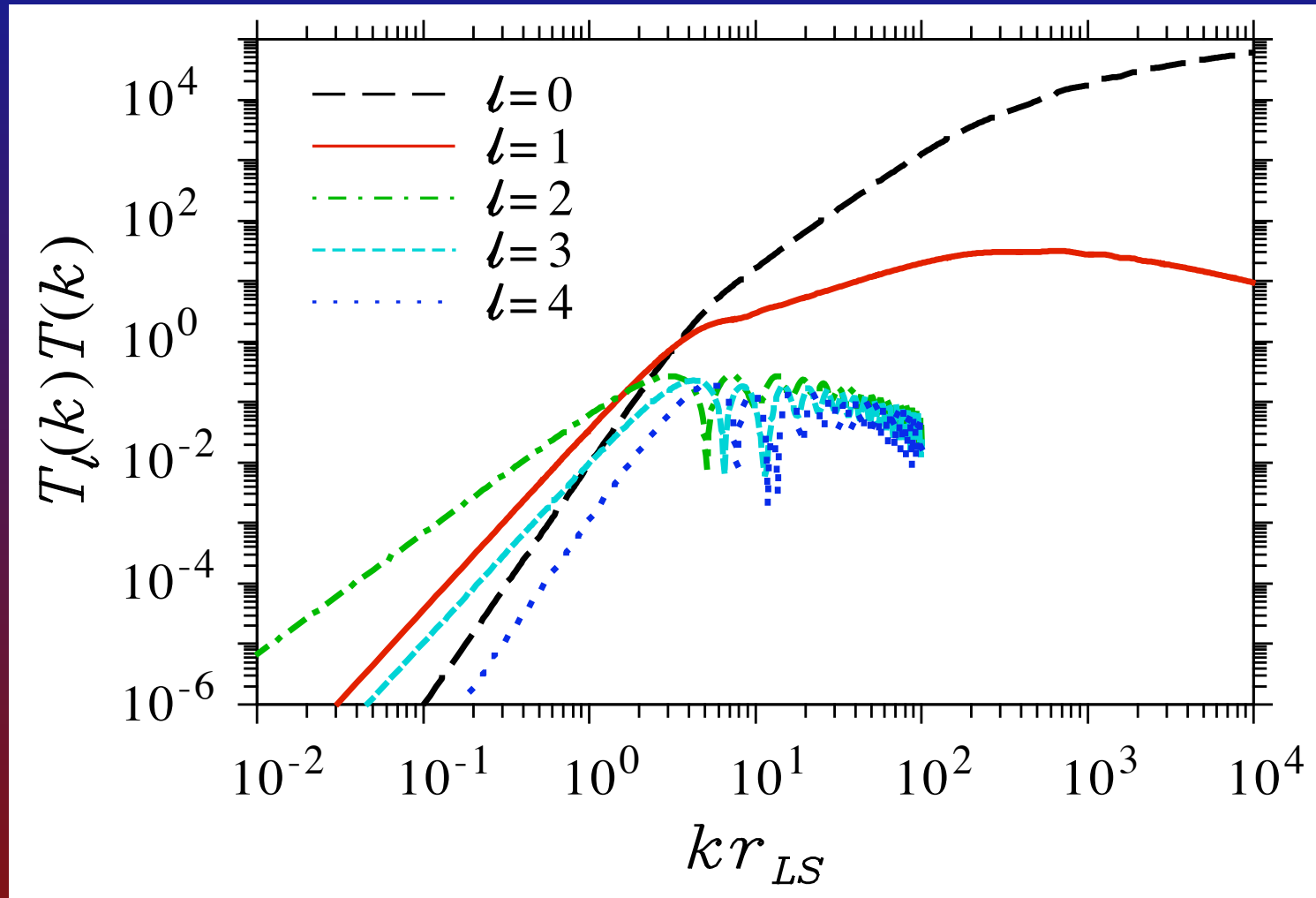
Monopole fluctuation is ambiguous -  
depends on choice of hypersurface  
(zero on constant radiation surface!)

Can still define monopole -  
through sensible coordinate choice

Obvious choice is uniform matter slice  
Or equivalently uniform energy density

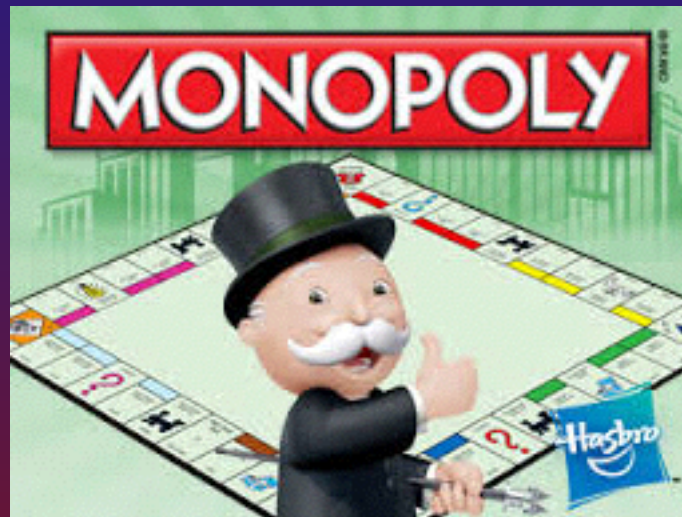
Can calculate the transfer function  
for the perturbations

Even if monopole (and dipole) coordinate-dependent  
... can still define the expected variance

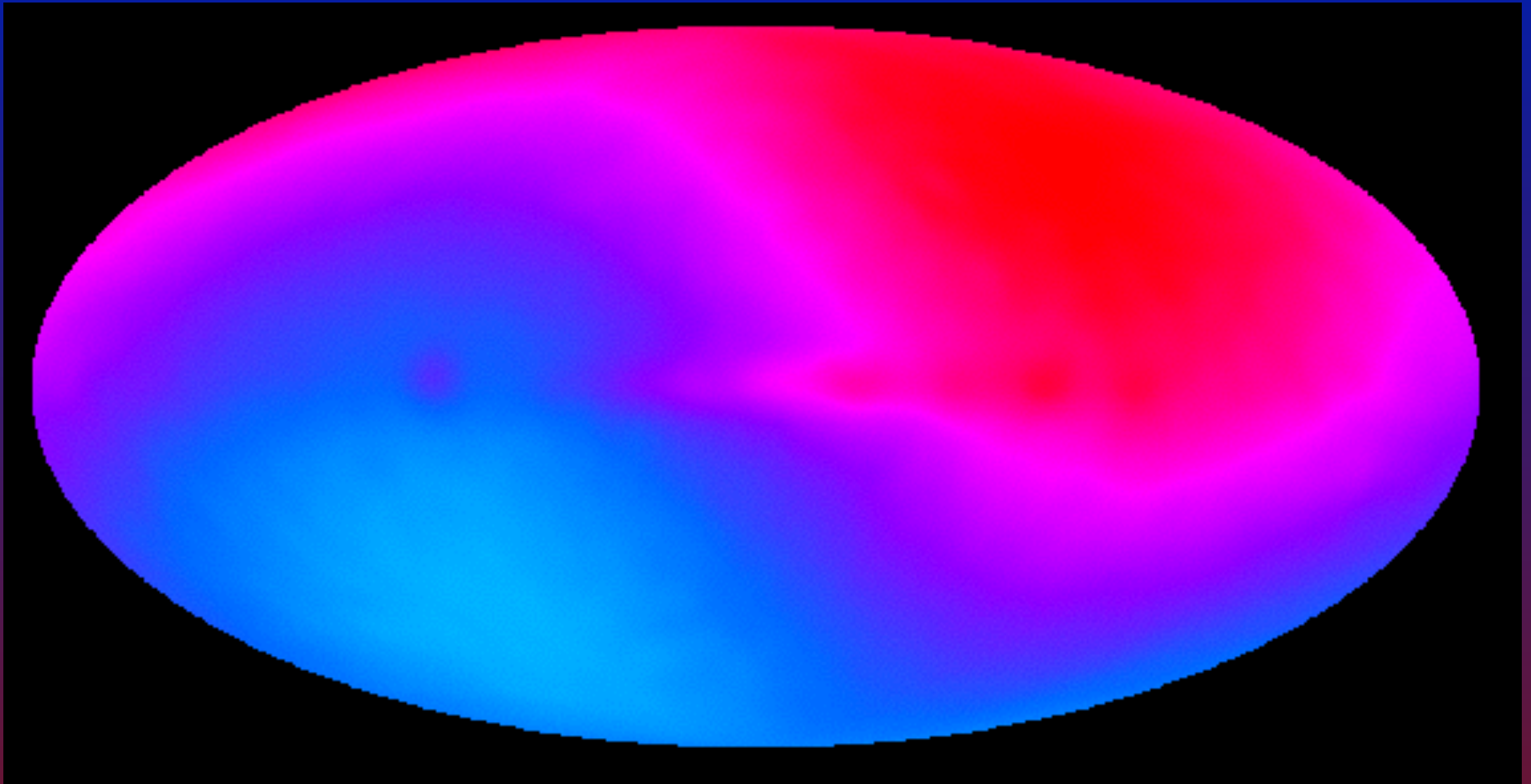


Find that monopole fluctuation is indeed  $\sim 10^{-5}$

What do you call the study of the monopole?



What about the dipole?  
... diplomacy?



CMB dipole (from COBE satellite)



# Defining the dipole

Dipole also ambiguous  
(zero in “CMB rest frame”!)

Choose comoving matter field

Large contribution from small-scales,  
which are non-linear  
(and Super-horizon contribution suppressed)

No “intrinsic dipole” for adiabatic perturbations  
(since matter frame = CMB frame)

# Defining the dipole

“Extrinsic” dipole comes from our motion

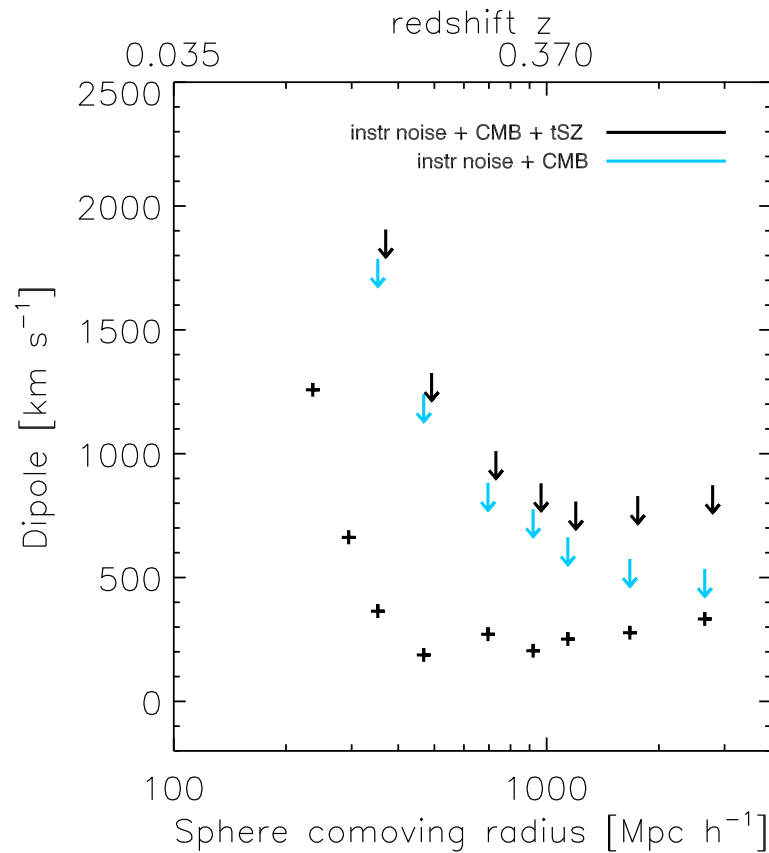
In principle estimate “real” motion with aberration

Or determine motion from accelerations due to local lumps of matter

Any deficit gives the dipole fluctuation (doesn't it?)

Not in adiabatic models!

The dipole is just our velocity relative to the CMB LSS



**Fig.9.** Bulk flow amplitude measured in *Planck* data with the all-sky method, after subtraction (vectorially) of the Galactic contribution (black crosses), compared with 95 % upper limits derived from simulations containing CMB and instrumental noise only (blue arrows) or also including tSZ signal (black arrows). The fact that the crosses are below the arrows at all scales shows that there is no significant bulk flow detection.

Planck  
intermediate  
paper XIII  
(arXiv:1303.5090)

Kinetic Sunyaev-  
Zeldovich effect

Places limit on  
large bulk flows

The matter and  
CMB frames are  
the same

# What about Planck's dipole?

The “orbital dipole” is used to calibrate  
So the “solar dipole” can be independently  
measured

This is the currently most precise dipole

Hence the best estimate of our velocity  
relative to the distance “rest frame”

# Planck's 2018 dipole

EXPERIMENT	AMPLITUDE [ $\mu\text{K}_{\text{CMB}}$ ]	GALACTIC COORDINATES	
		$l$ [deg]	$b$ [deg]
COBE <sup>a</sup> . . . . .	3358 $\pm$ 24	264.31 $\pm$ 0.20	48.05 $\pm$ 0.11
WMAP <sup>b</sup> . . . . .	3355 $\pm$ 8	263.99 $\pm$ 0.14	48.26 $\pm$ 0.03
<i>Planck</i> 2015 nominal <sup>c</sup> . . . . .	3364.5 $\pm$ 2.0	264.00 $\pm$ 0.03	48.24 $\pm$ 0.02
LFI 2018 <sup>d</sup> . . . . .	3364.4 $\pm$ 3.1	263.998 $\pm$ 0.051	48.265 $\pm$ 0.015
HFI 2018 <sup>d</sup> . . . . .	3362.08 $\pm$ 0.99	264.021 $\pm$ 0.011	48.253 $\pm$ 0.005
<b><i>Planck</i> 2018 <sup>e</sup> . . . . .</b>	<b>3362.08 <math>\pm</math> 0.99</b>	<b>264.021 <math>\pm</math> 0.011</b>	<b>48.253 <math>\pm</math> 0.005</b>

Position now known to  $\sim 30''$

(uncertainties are systematics dominated)

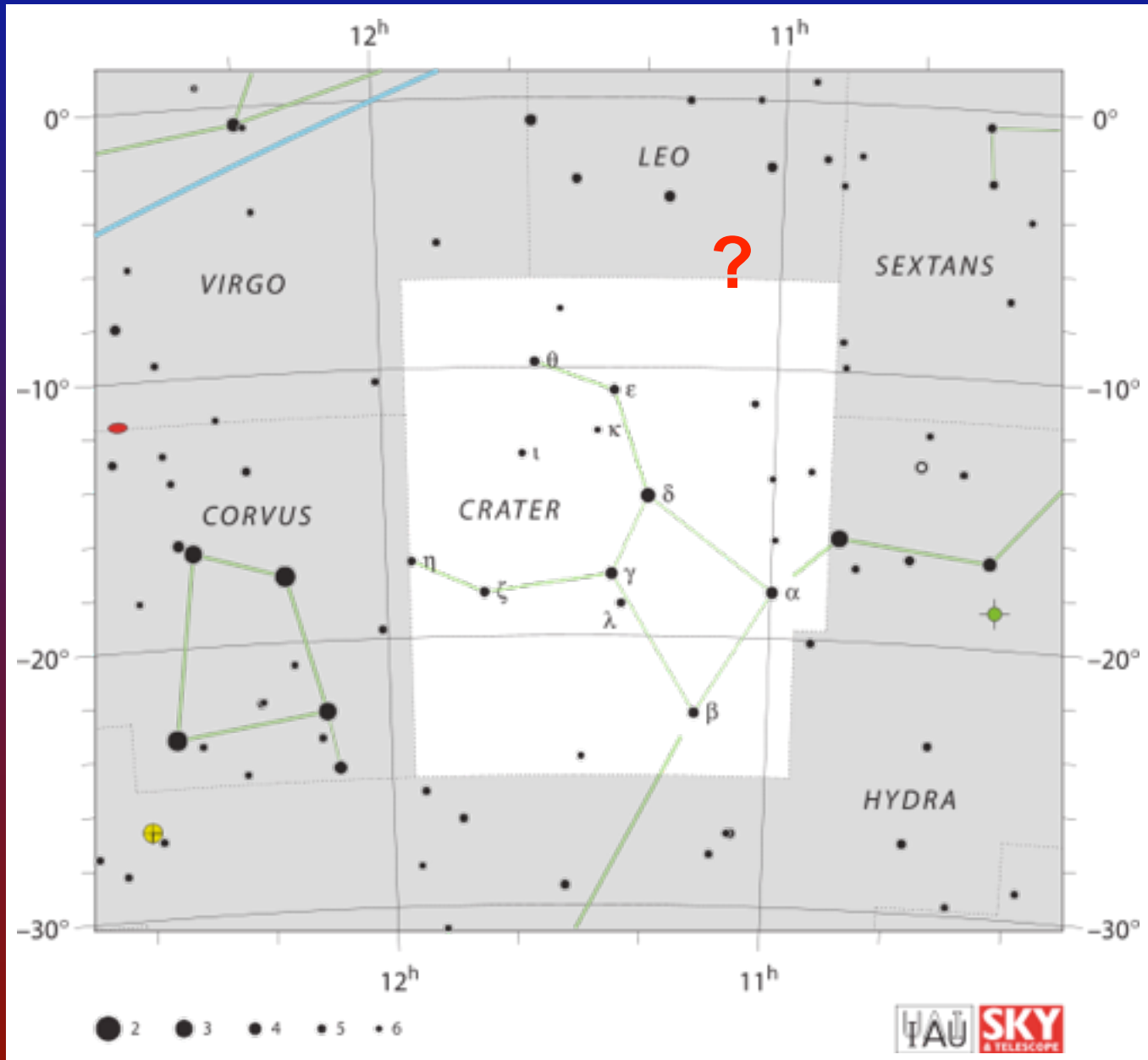
Planck's 2015 dipole amplitude:

$$v = 0.12345\% c !$$

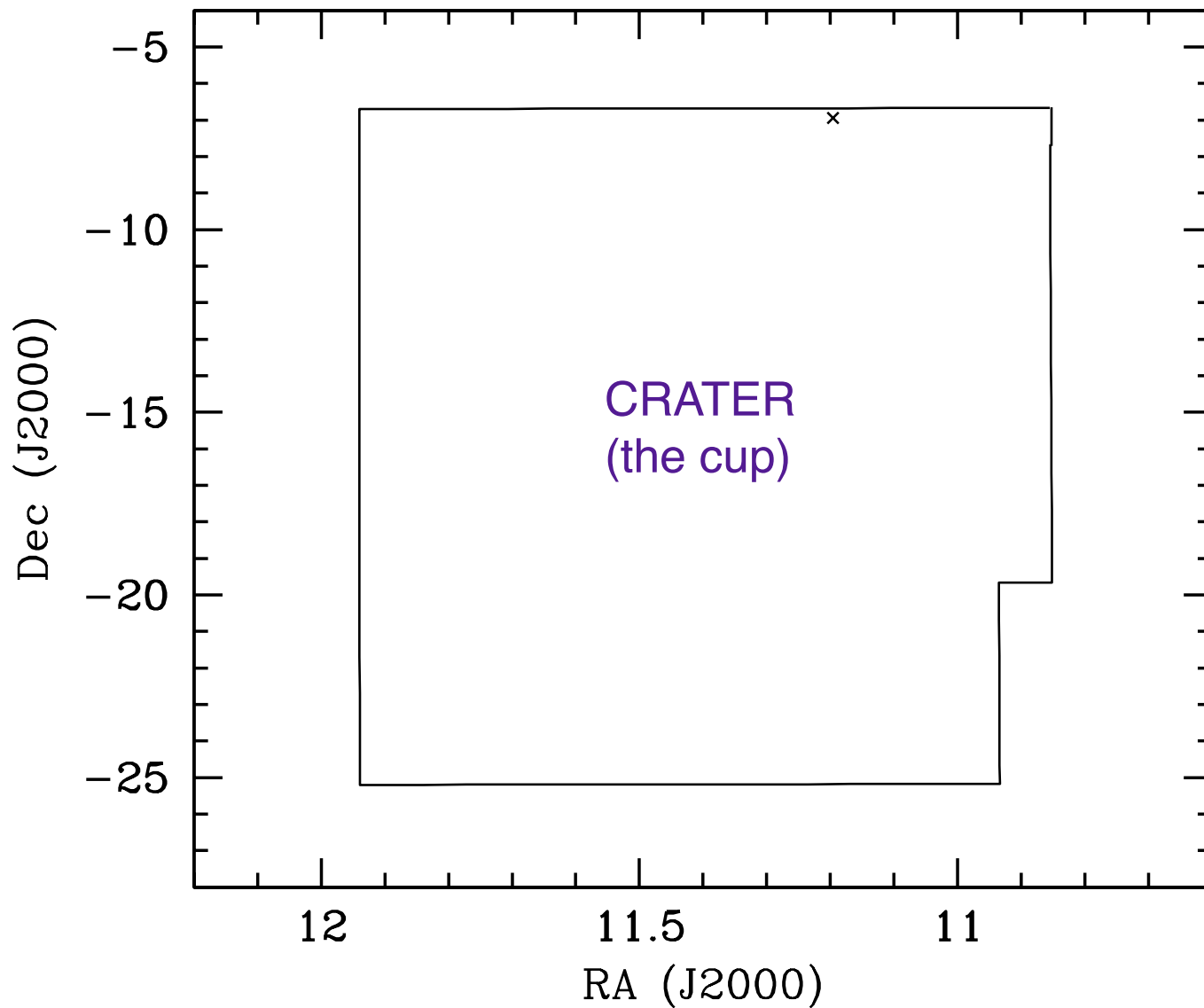
Planck's 2018 dipole amplitude:

$$v = (0.12336 \pm 0.00004)\% c$$

# Where's the dipole direction?



# What constellation am I in?





**Table 3.** Relative velocities involving the CMB frame, the Galactic centre, and the Local Group.

**Cosmologists should care most about this number**

Relative velocity	Speed [km s <sup>-1</sup> ]	<i>l</i> [deg]	<i>b</i> [deg]
Sun–CMB <sup>a</sup> . . . . .	369.82 ± 0.11	264.021 ± 0.011	48.253 ± 0.005
Sun–LSR <sup>b</sup> . . . . .	17.9 ± 2.0	48 ± 7	23 ± 4
LSR–GC <sup>c</sup> . . . . .	239 ± 5	90	0
GC–CMB <sup>d</sup> . . . . .	565 ± 5	265.76 ± 0.20	28.38 ± 0.28
Sun–LG <sup>e</sup> . . . . .	299 ± 15	98.4 ± 3.6	-5.9 ± 3.0
LG–CMB <sup>d</sup> . . . . .	620 ± 15	271.9 ± 2.0	29.6 ± 1.4

<sup>a</sup> Velocity of the Sun relative to the CMB; *Planck* 2018.

<sup>b</sup> Velocity of the Sun relative to the Local Standard of Rest from [Schönrich et al. \(2010\)](#), adding the statistical and systematic uncertainties.

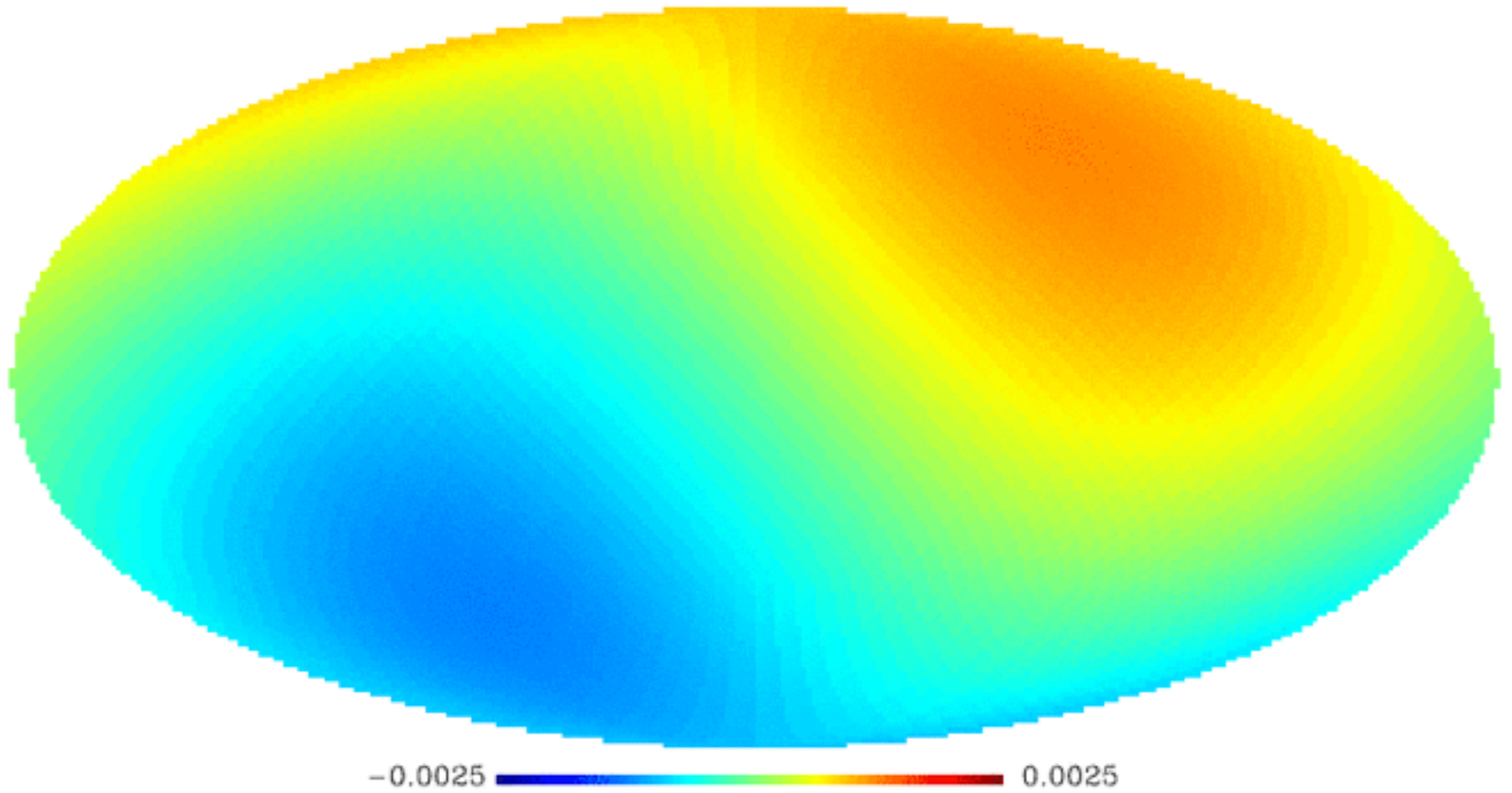
<sup>c</sup> Rotational velocity of the LSR from [McMillan \(2011\)](#).

<sup>d</sup> Resulting velocity, using non-relativistic velocity addition and assuming uncorrelated errors.

<sup>e</sup> Velocity of the Sun relative to the Local Group from [Diaz et al. \(2014\)](#).

# Dipole evolves as we circle the Galaxy

test\_000.fits: SIMULATION



# Recall issues relevant to monopole and dipole

- Monopole:  $T_0=(2.7255\pm 0.0006)\text{K}$
- CMB last-scattering surface defines a rest frame
- It's the frame with no observable dipole
- Relative to that frame we're moving at  $\approx 370\text{km/s}$
- $\beta=0.0012345$  towards the constellation Crater
- Local Group  $620\text{km/s}$  relative to CMB

And there are other effects...

# And there are other effects...

- Dipole-modulate monopole → CMB dipole Well known!
- Dipole-modulation of all other multipoles Planck 2013
- Aberration of anisotropies Planck 2013
- Increase in monopole by  $\beta^2/6$  Unmeasurable
- Generation of  $O(\beta^2)$  quadrupole  $l$  spectrum?

And related effects at other wavelengths,  
e.g. modulation of source counts

# Detection of the velocity dipole in the radio galaxies of the NRAO VLA Sky Survey

Chris Blake, Jasper Wall (Oxford University)

*(Submitted on 21 Mar 2002)*

We are in motion against the cosmic backdrop. This motion is evidenced by the systematic temperature shift – or dipole anisotropy – observed in the Cosmic Microwave Background radiation (CMB). Because of the Doppler effect, the temperature of the CMB is 0.1 per cent higher in our direction of motion through the Universe. If our standard cosmological understanding is correct, this dipole should also be present as an enhancement in the surface density of distant galaxies. The main obstacle in finding this signal is the very uneven distribution of nearby galaxies in the Local Supercluster, which drowns out the small cosmological imprint. Here we report the first detection of the expected dipole anisotropy in the galaxy distribution, in a survey of galaxies detected in radio waves. Radio galaxies are mostly located at cosmological distances, so the contamination from nearby clusters should be small. With local radio sources removed, we find a dipole anisotropy in the radio galaxy distribution in the same direction as the CMB, close to the expected amplitude. This result is confirmation of the standard cosmological interpretation of the CMB.

Comments: Published in Nature 416, p.150 (12 pages)

Subjects: **Astrophysics (astro-ph)**

DOI: [10.1038/416150a](https://doi.org/10.1038/416150a)

Cite as: [arXiv:astro-ph/0203385](https://arxiv.org/abs/astro-ph/0203385)

(or [arXiv:astro-ph/0203385v1](https://arxiv.org/abs/astro-ph/0203385v1) for this version)

Jasper (and Chris') dipole contribution

# Boosting frames

observed frame

CMB frame

Now  $T(\hat{n}) = \frac{T'(\hat{n}')}{\gamma(1 - \hat{n} \cdot \beta)}$   $\leftarrow v/c$

with  $\hat{n} = \frac{\hat{n}' + [(\gamma - 1)\hat{n}' \cdot \hat{v} + \gamma\beta]}{\gamma(1 + \hat{n}' \cdot \beta)}$

To 1st order in  $\beta$ :

$$T'(\hat{n}') = T'(\hat{n} - \nabla(\hat{n} \cdot \beta)) \equiv T_0 + \delta T'(\hat{n} - \nabla(\hat{n} \cdot \beta))$$

So finally:

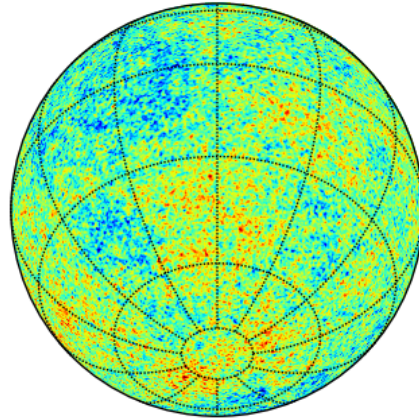
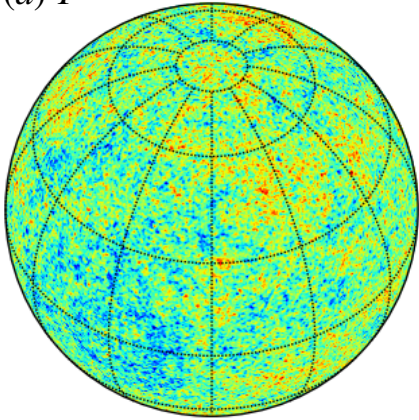
$$\delta T(\hat{n}) = \underbrace{T_0 \hat{n} \cdot \beta}_{\text{dipole}} + \delta T'(\hat{n} - \underbrace{\nabla(\hat{n} \cdot \beta)}_{\text{deflections}})$$

```
\def\mathbi#1{\textbf{\em #1}}
T(\hat{\mathbi{n}}) = T^\wedge
\prime(\hat{\mathbi{n}})^\prime
\over \gamma(1-\hat{\mathbi{n}}
\prime\cdot\mbox{\boldr
\beta$}
```

```
\def\mathbi#1{\text
{\hat{\mathbi{n}},}}
{\hat{\mathbi{n}},}}
\left[(\gamma-1)
{\hat{\mathbi{n}},}}
\cdot{\hat{\mathbi{n}}
+ \gamma\beta\text{rig
{\hat{\mathbi{v}},}}
\gamma(1+{\hat{\n}
\prime\cdot\mbox{
{\boldmath$\beta$}
```

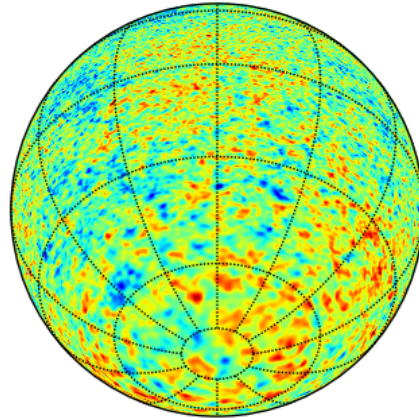
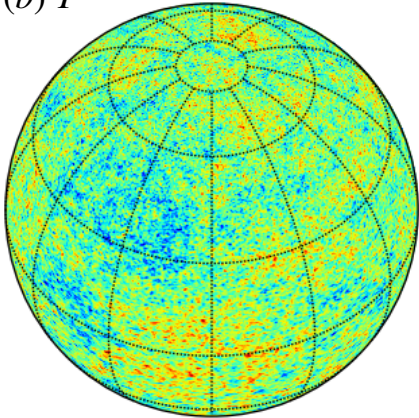
```
\def\mathbi#1{\textbf{\em
T^\wedge\prime(\hat{\mathbi{n},
\prime) = T^\wedge\prime(\hat{\n
\prime)-\nabla(\hat{\mathbi{n}
\cdot\mbox{\boldmath$\b
\equiv T_0 + \delta T^\wedge
\prime(\hat{\mathbi{n},}}
\prime(\hat{\mathbi{n},}}
\prime)\nabla(\hat{\mathbi{n},}}
```

(a)  $T^{\text{PRIMORDIAL}}$



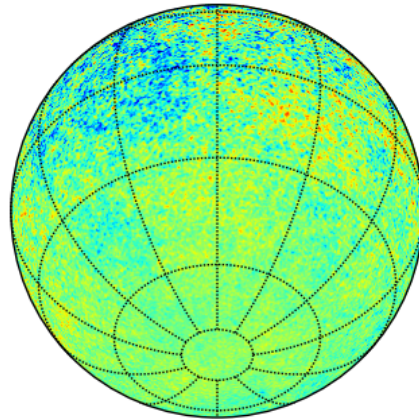
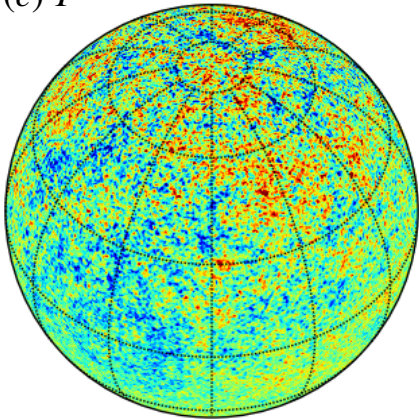
Simulated CMB

(b)  $T^{\text{ABERRATION}}$



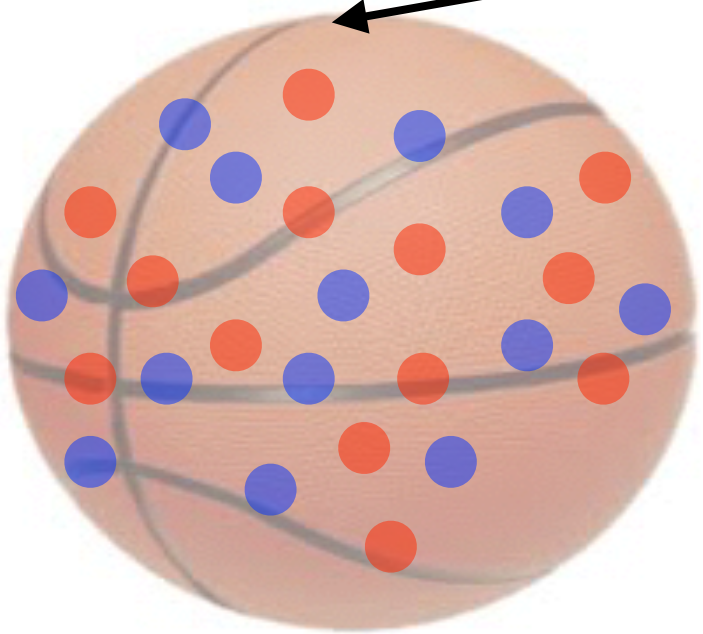
Aberration  
for  $\beta=0.85$

(c)  $T^{\text{MODULATION}}$

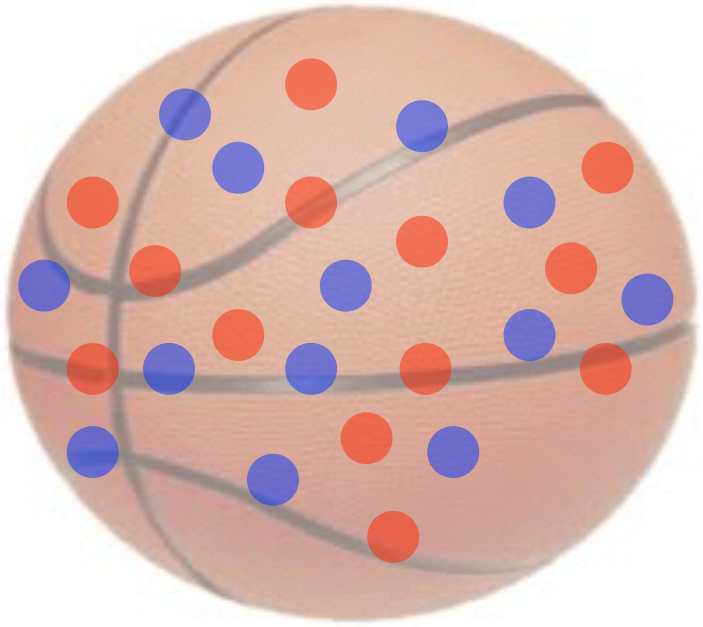
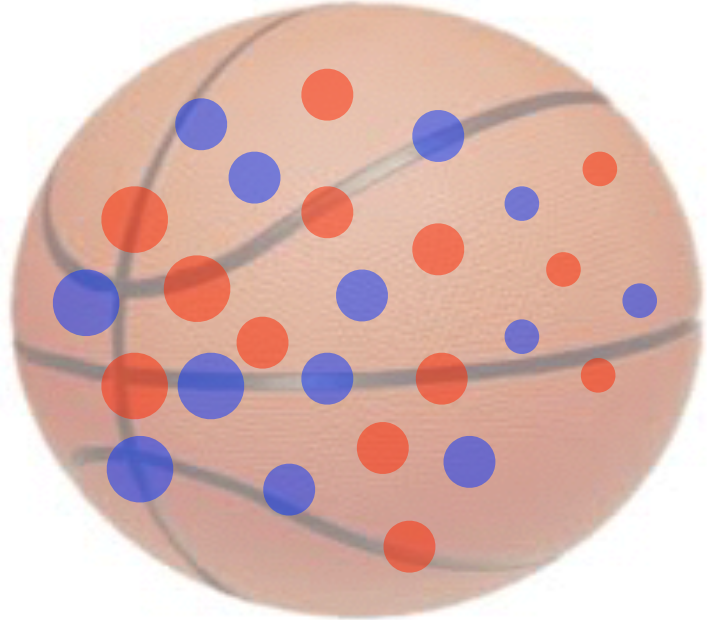


Modulation  
for  $\beta=0.85$

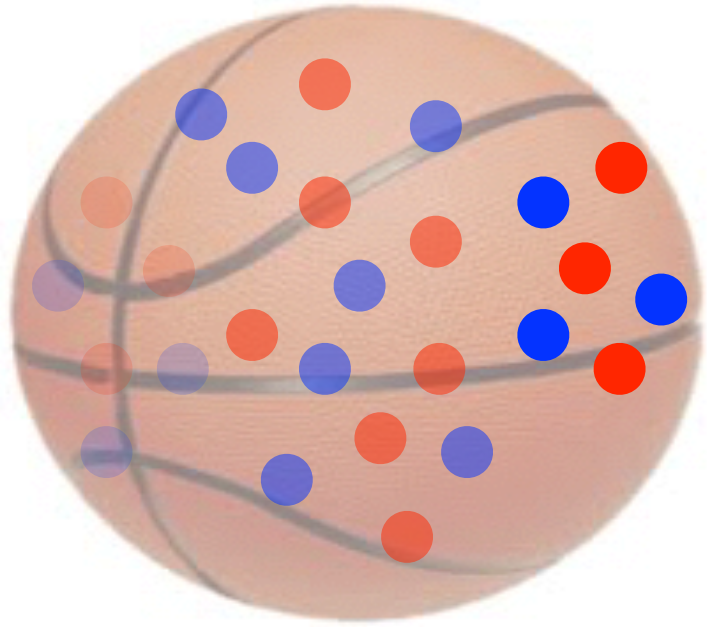
Valve?



Aberration



Modulation





# Boosting frames

With *Planck* we can try to measure both the aberration and boosting effects

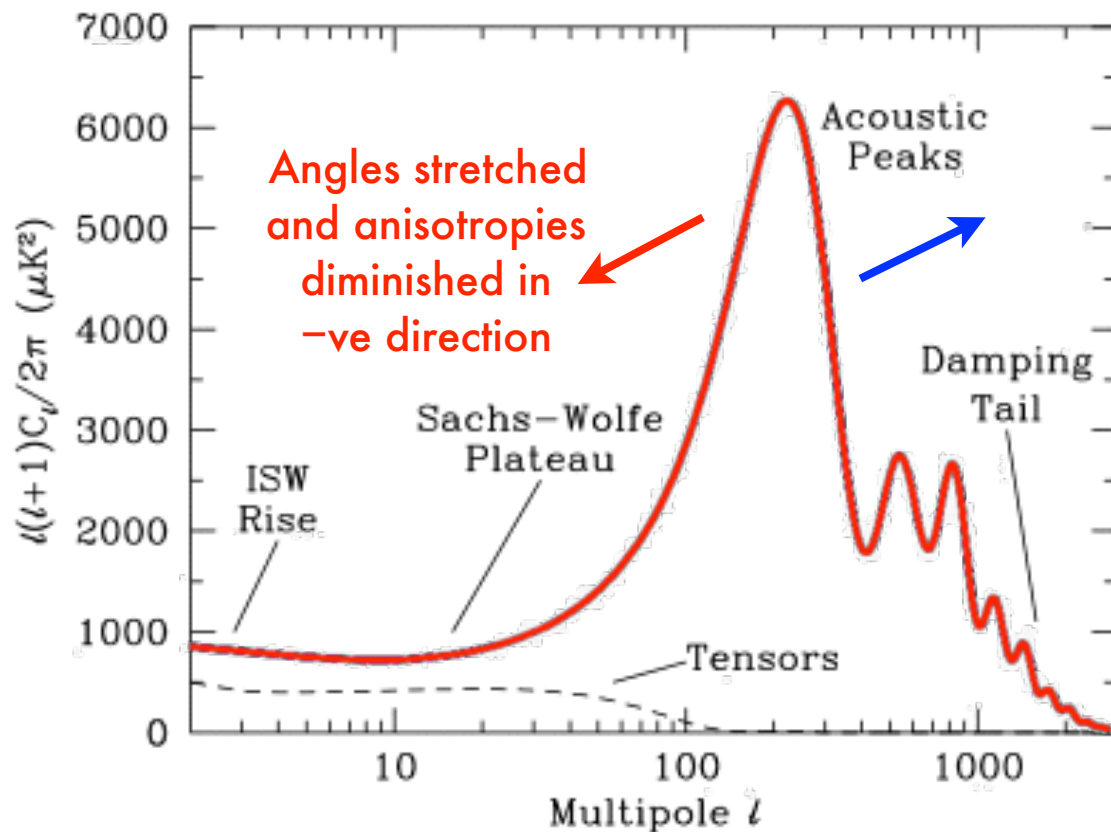
This could be or l p space

$$\begin{aligned} & \left( \frac{\hat{n}' + \gamma \beta \hat{v}}{\gamma (1 + \beta \hat{n} \cdot \hat{v})} \right) \\ & = \frac{\hat{n}' + \gamma \beta \hat{v}}{\gamma (1 + \beta \hat{n} \cdot \hat{v})} \end{aligned}$$

Harmonic space is more efficient and uses machinery of  $\langle T_1 T_2 T_3 T_4 \rangle$

$$\begin{aligned} & T(\hat{n}) - \frac{\hat{n}' + \gamma \beta \hat{v}}{\gamma (1 + \beta \hat{n} \cdot \hat{v})} \\ & = \frac{\hat{n}' + \gamma \beta \hat{v}}{\gamma (1 + \beta \hat{n} \cdot \hat{v})} - \hat{n} \end{aligned}$$

# Boosting frames



Angles squashed  
and anisotropies  
boosted in  
+ve direction

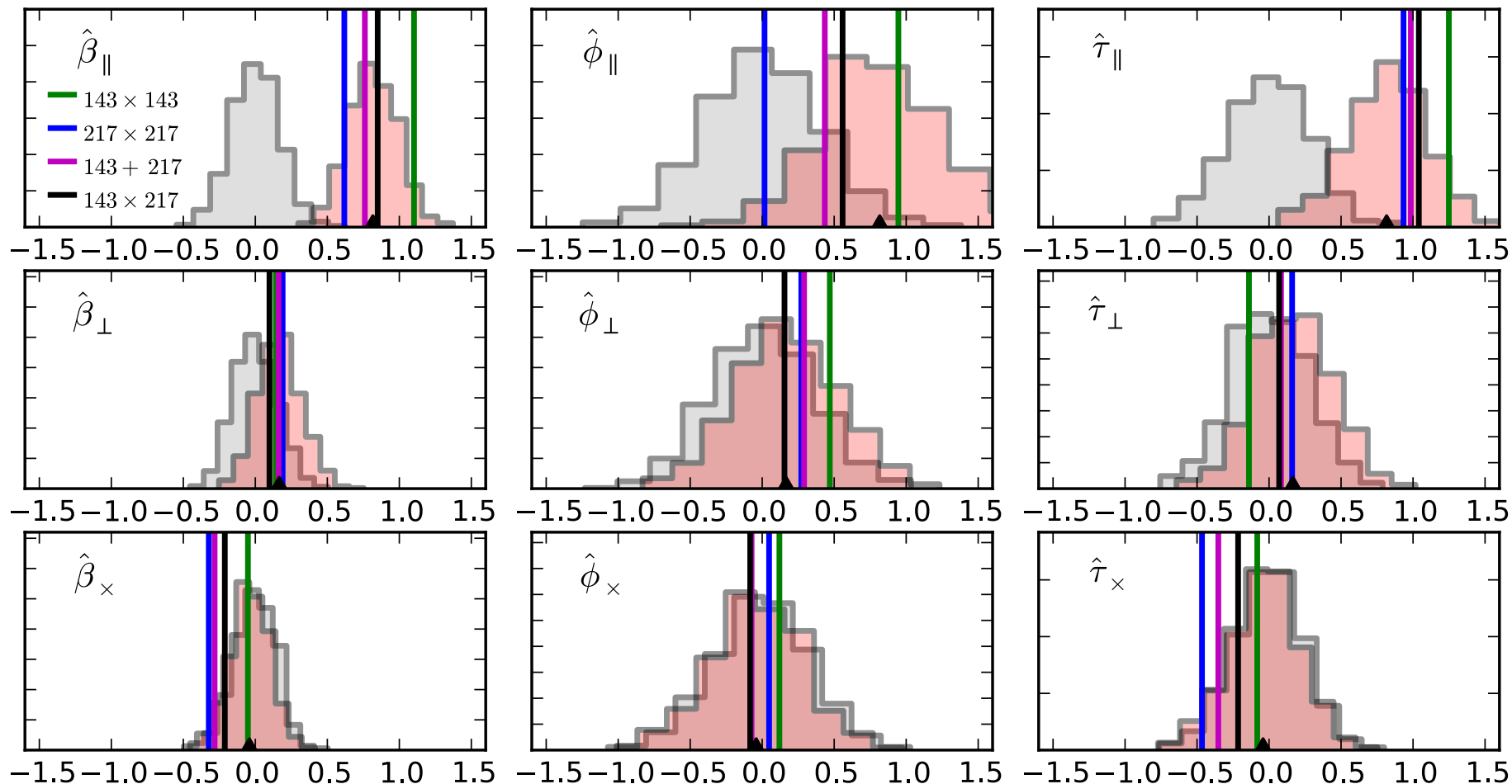
Or can consider this as an effect which  
couples harmonics

This was measured convincingly in 2013 Planck data set

# Total

# Aberration

# Modulation



Grey histogram: without Pink histogram: with  $\beta$  effects

Vertical lines are different data combinations

# So what?

- Velocity Measured at  $4-5\sigma$
- (Complication with hemispheric asymmetry)
- Slightly biases parameters for partial sky coverage
- Probably doesn't tell us anything new, but it's cute!
- Only possible with *Planck*!

"Eppur si muove"  
[And yet it moves]



Are these “boosting” effects  
actually interesting?

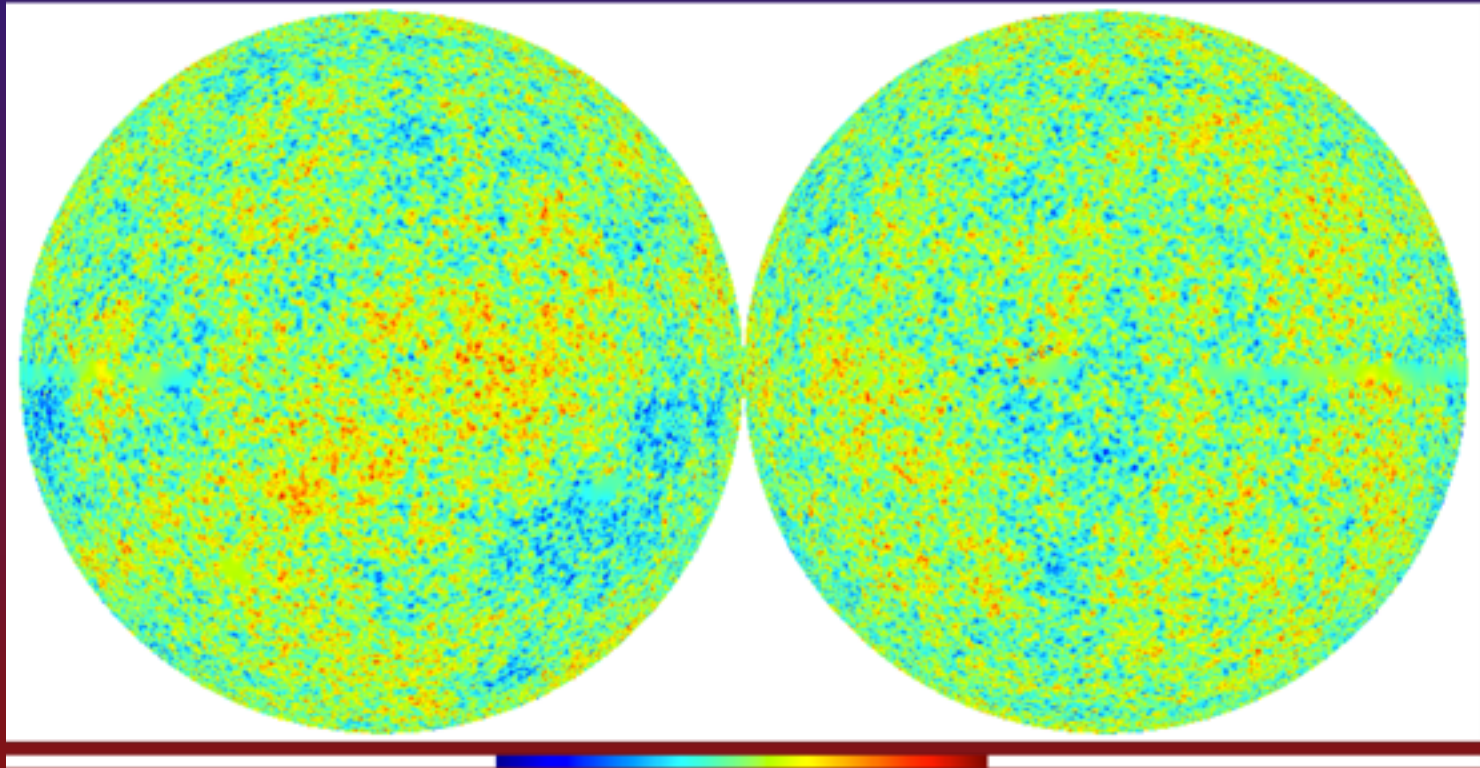
Could we tell about an  
“intrinsic dipole”?

No, because you’d get these  
effects with any dipole!

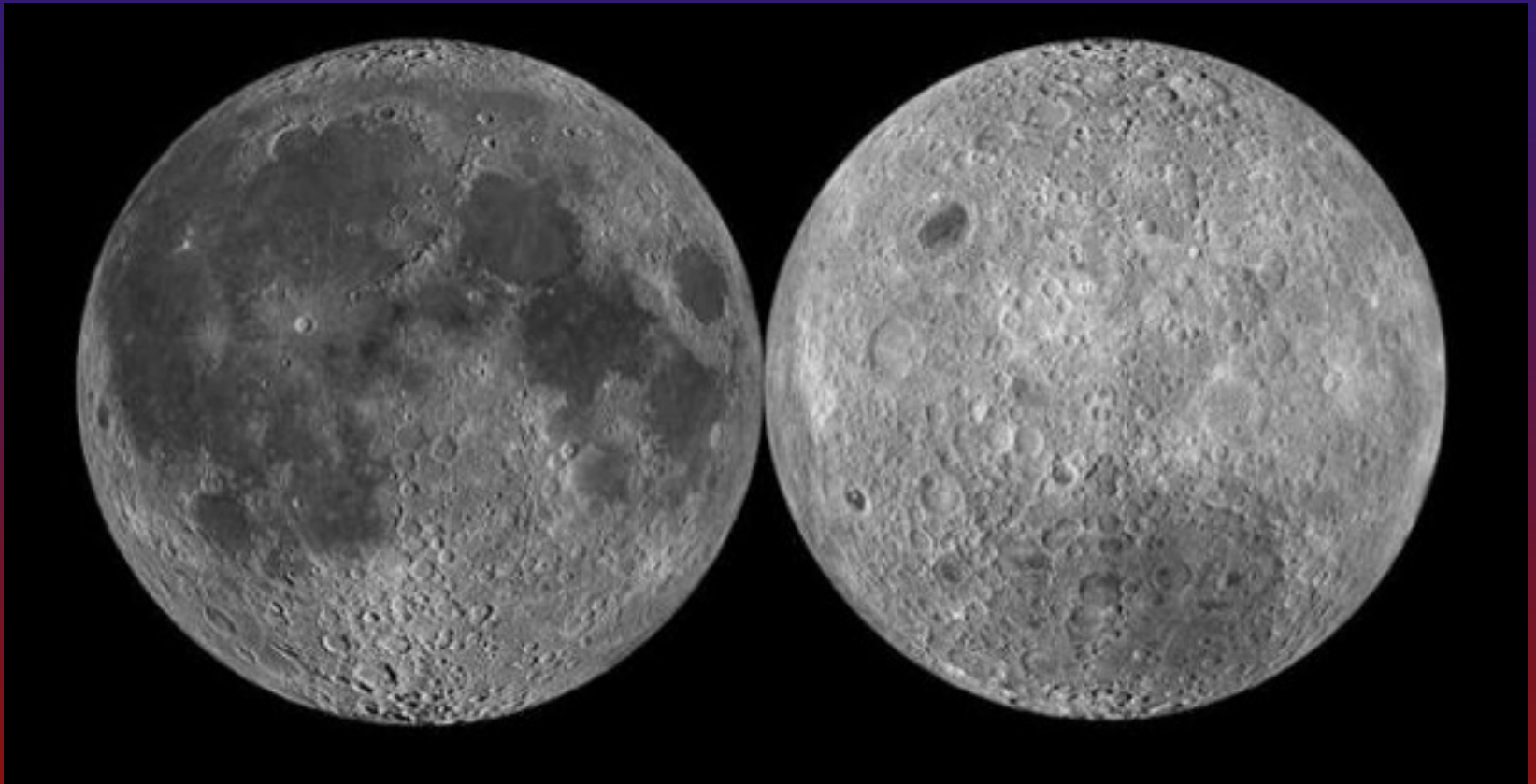
Sky appears dipole-  
modulated  
at large angular scales  
(see Planck 2015 I&S paper)

Not caused by velocity  
(only large scales)  
- is it statistically significant?

Do the 2 sides of the  
CMB sky look alike?



Do the 2 sides of the  
Moon look alike?





Dipole modulation/  
hemispheric asymmetry  
is real, but subtle

Maps modulated by  $\approx 6\%$ ,  
but only out to  $l_{\max} \approx 64$

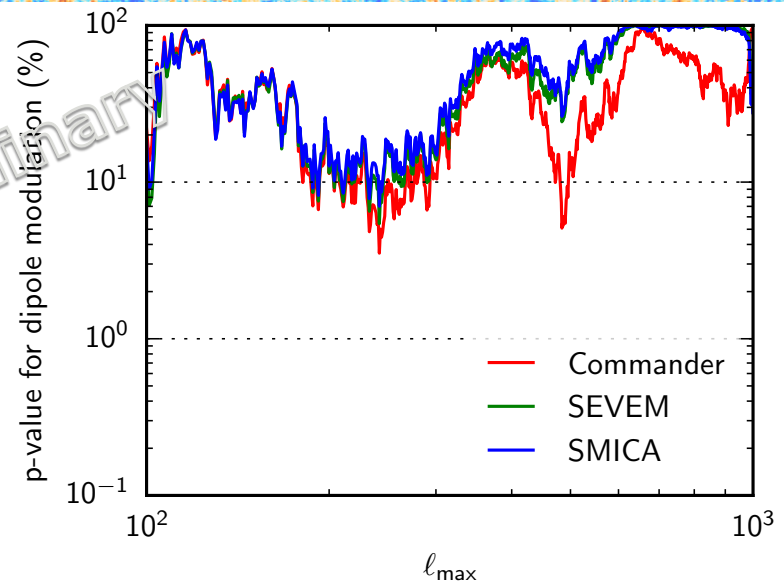
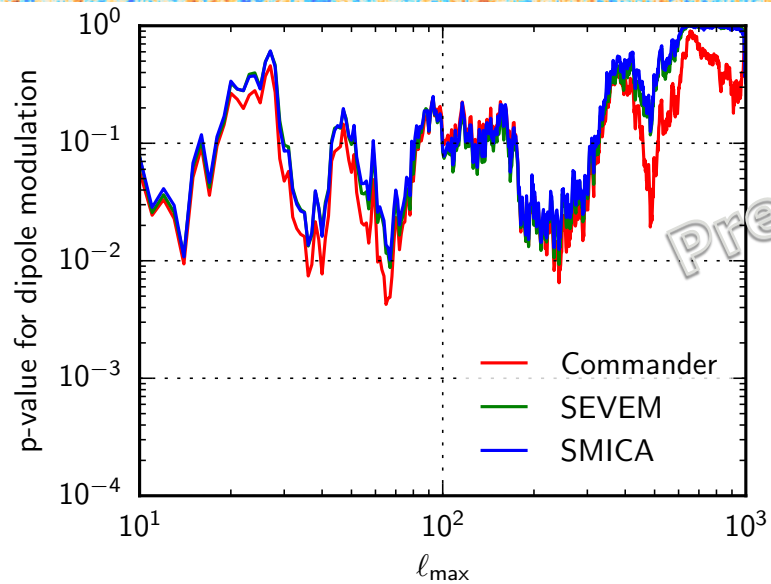
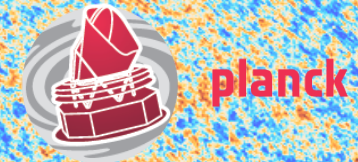
How do we assess  
whether this is  
statistically unlikely?

“Cosmic variance”  
expectation for  
dipole modulation to  $\ell_{\max}$  :

$$\left\langle \frac{\Delta A_s}{A_s} \right\rangle \approx \sqrt{\frac{48}{\pi(\ell_{\max} + 4)(\ell_{\max} - 1)}}.$$

Map modulation is half of  
this, e.g. 2.9% for  $\ell_{\max}=67$

# Dipolar power modulation: harmonic analysis



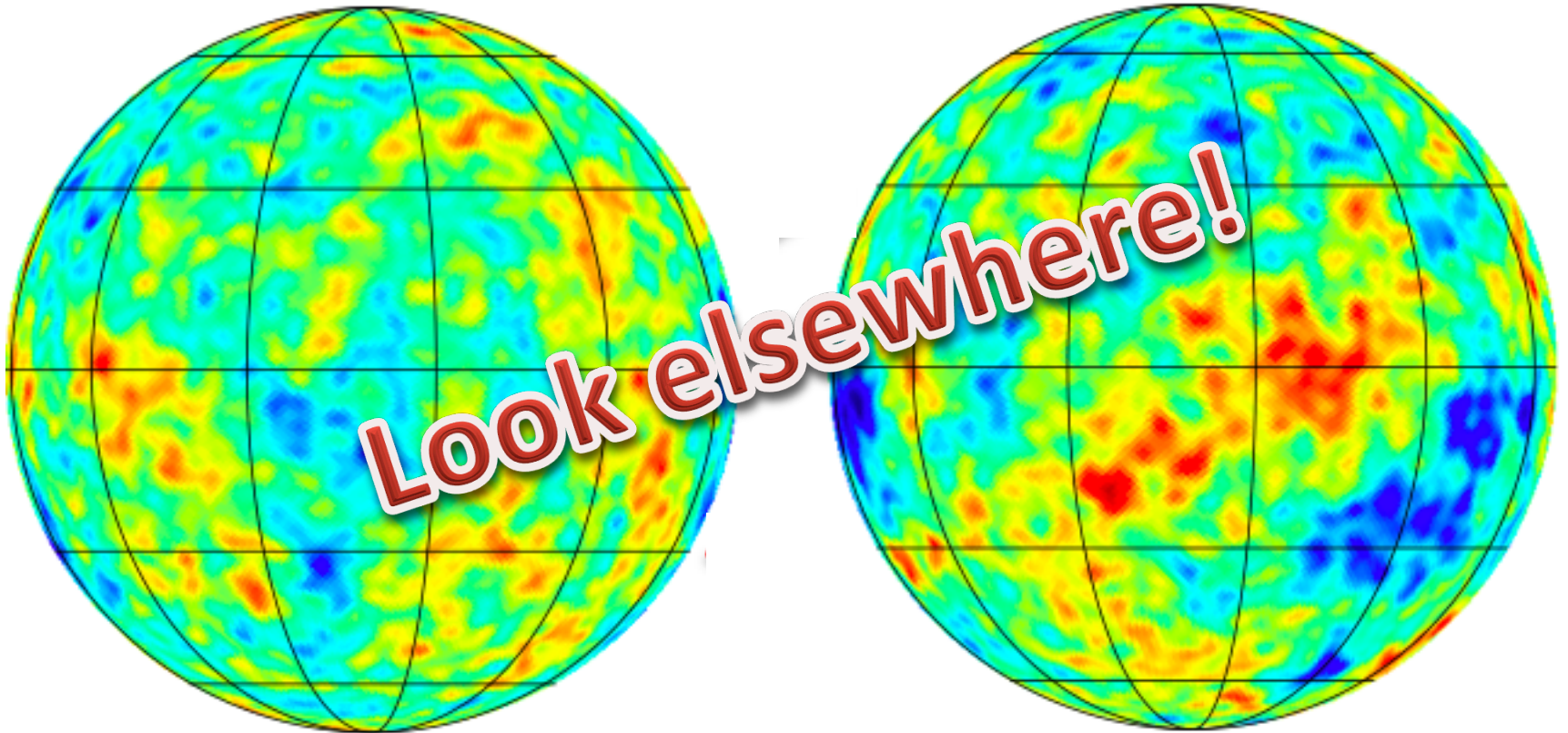
We use the harmonic QML estimator introduced in Moss et al 2011 (see also The Planck Collaboration, 2014, 571:A17-A27) to *Planck* intensity maps.

For  $l_{\min}=2$  we found a  $\sim 3\sigma$  dipole modulation at  $l_{\max} \sim 65$  with a  $\sim 6.3\%$  amplitude.

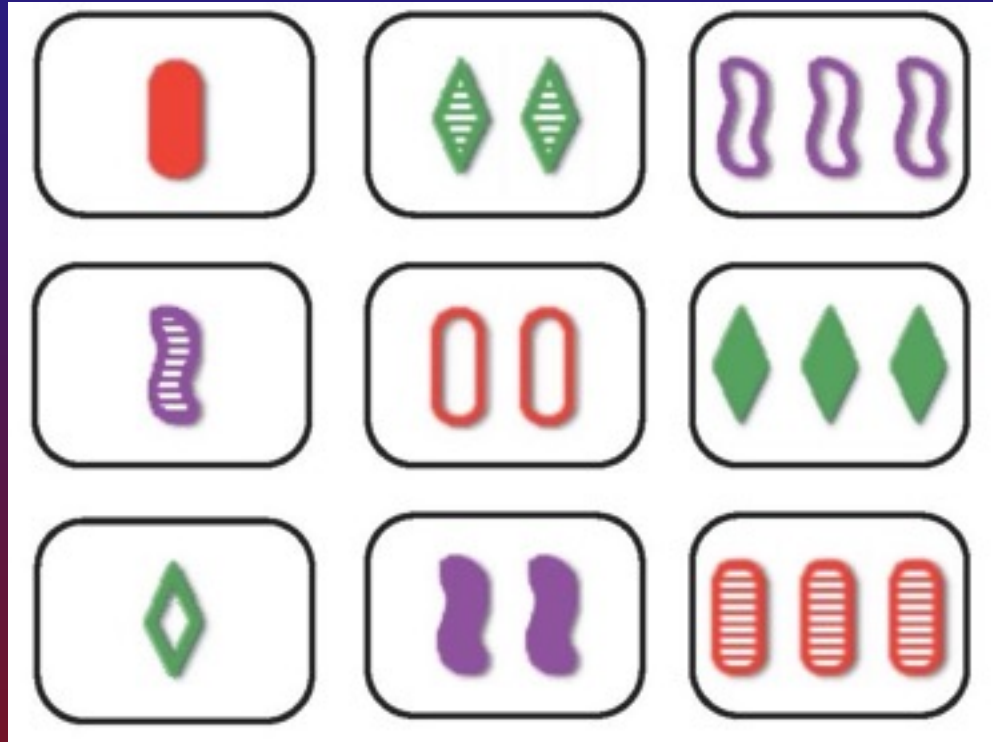
There is also evidence for modulations at  $l_{\max} \sim 40$ , and  $l_{\max} \sim 240$ .

However, the latter becomes much less significant when adopting  $l_{\min}=100$ , i.e. removing large angular scales.

## *Large Angle Anomalies*



Our sky might look like this  
deal from the game "Set"



You should only get excited  
if it looks like this!

Right now the result doesn't  
look very remarkable

But if we had a predictive model  
that would change everything

Large scales are special, so  
we should keep looking

Polarization offers the promise  
of an independent test

Quadrupole:  
also some special issues  
but out of time ...

Other backgrounds  
will also give dipoles

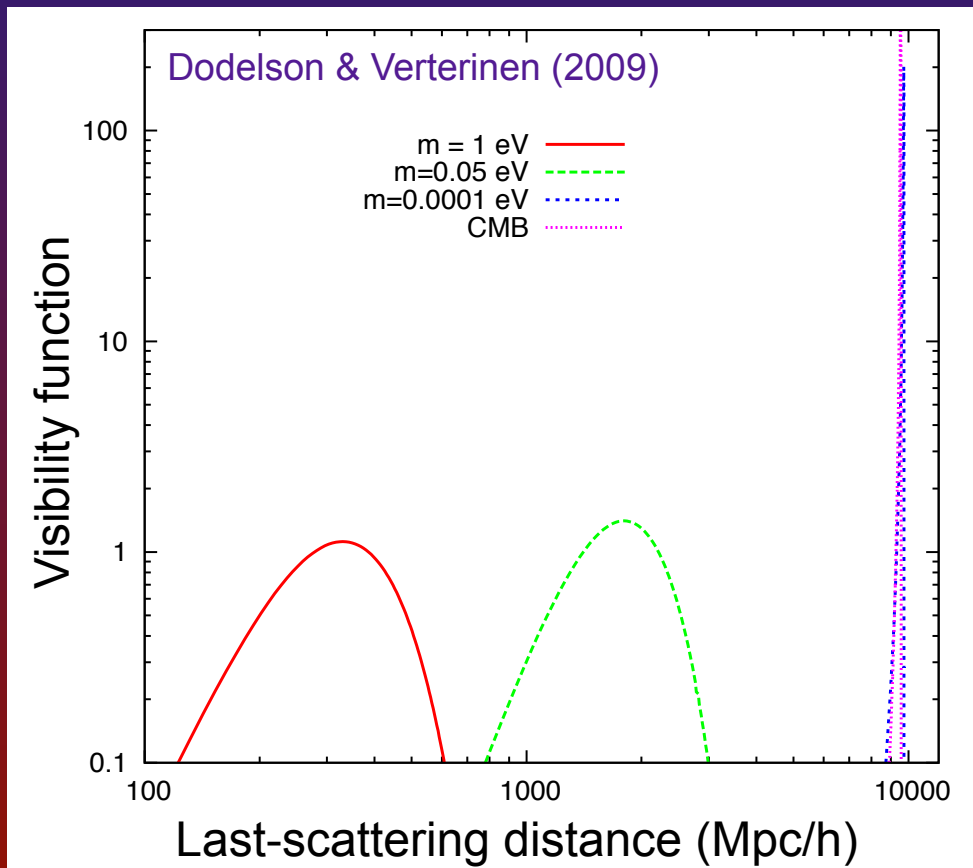
Depends on monopole  
and spectral shape

Radio dipole, optical dipole,  
and neutrino dipole?



# Neutrino dipole?

Cosmic neutrino background is 1.9K (and F-D)  
3 flavour states decoupled at about 1 second  
But last-scattering surface(s) complicated!



Each mass state has a different LSS distance

And thick, because of momentum distribution

Dipole for lowest  $m$  could be affected by gravitational lensing

The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada.



Planck is a project of the European Space Agency, with instruments provided by two scientific Consortia funded by ESA member states (in particular the lead countries: France and Italy) with contributions from NASA (USA), and telescope reflectors provided in a collaboration between ESA and a scientific Consortium led and funded by Denmark.